

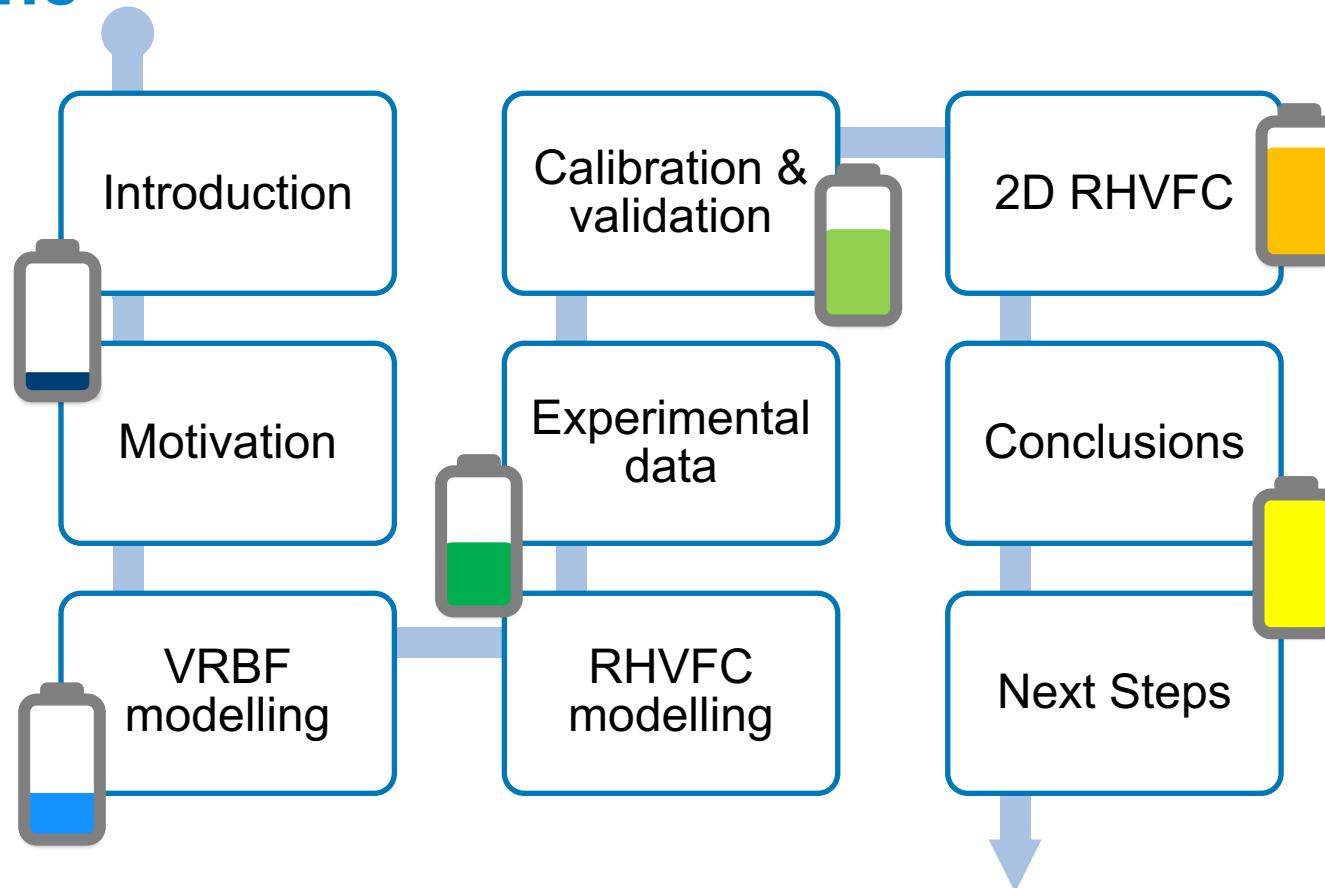
Modelling of a Regenerative Hydrogen-Vanadium Fuel Cell

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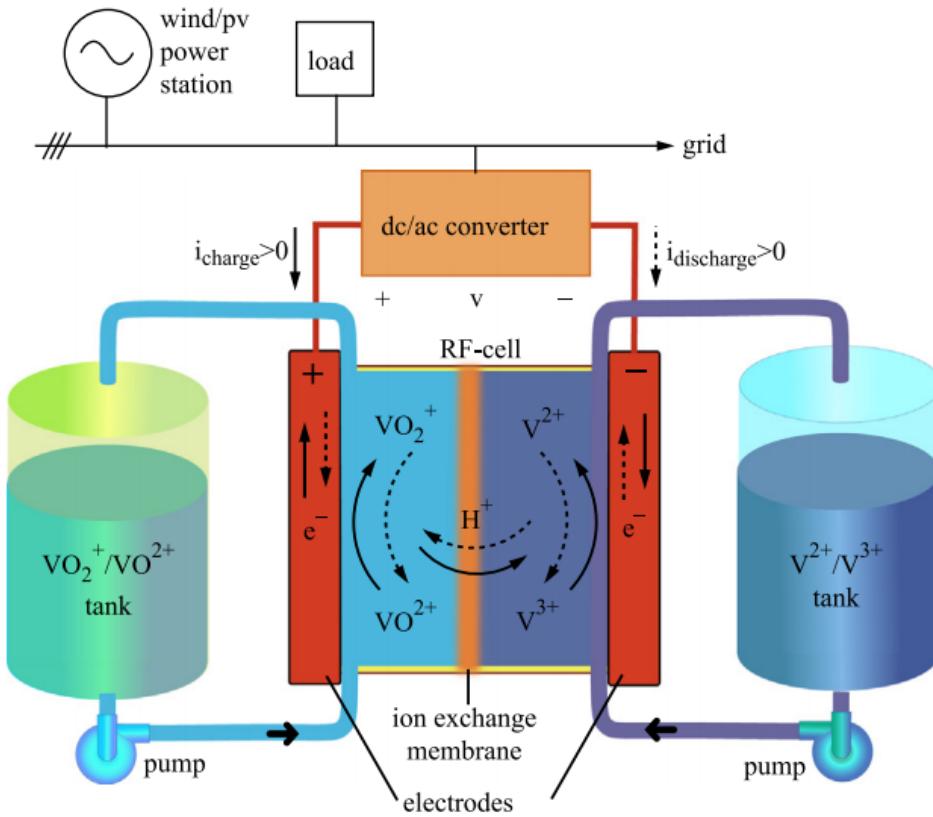
June 6th, 2018

Outline





Vanadium Redox Flow Battery (VRFB)



Vanadium based RFB

- Vanadium / halide
 - Vanadium / air
- Anolyte $V(II)$ / $V(III)$

Advantages

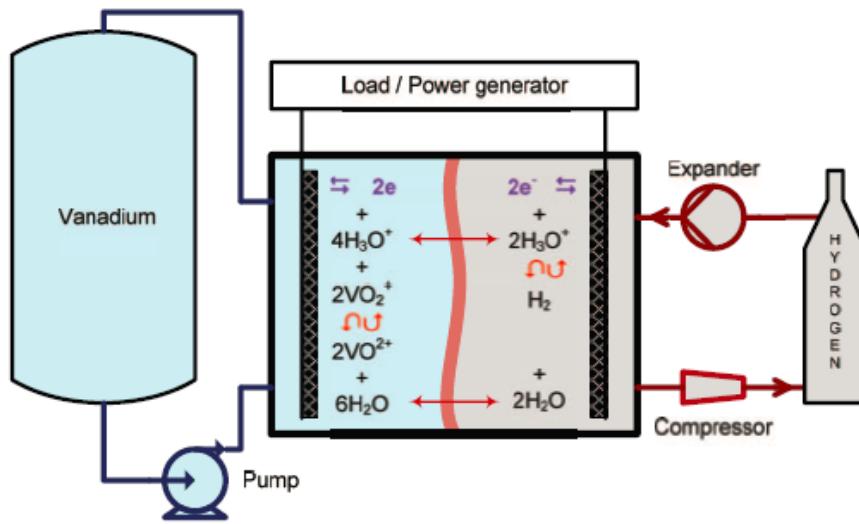
- Scalability and flexibility
- Independent sizing of power and energy
- High round-trip efficiency (>80%)
- Depth of discharge
- Long cycle life (>12000)
- Fast response
- Reduced environmental impact

Disadvantages

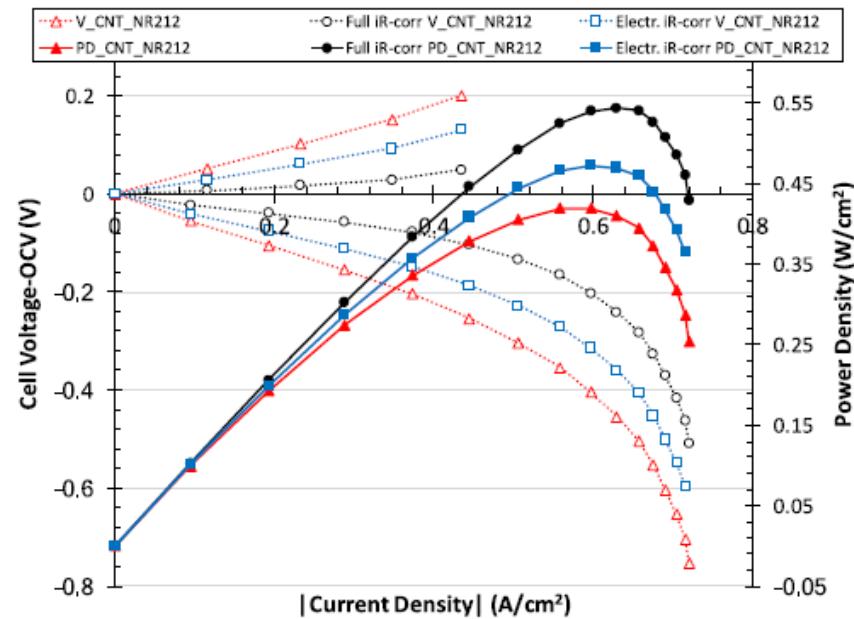
- Low specific energy density (~30 Wh kg⁻¹)
- Limited operating window (10-40 °C below 2 M)
- Electrode and membrane degradation
- Shunt currents
- High capital cost (\$150-\$1000/kWh)
- Vanadium electrolyte ~40% total cost



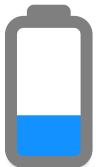
Regenerative Hydrogen-Vanadium Fuel Cell (RHVFC)



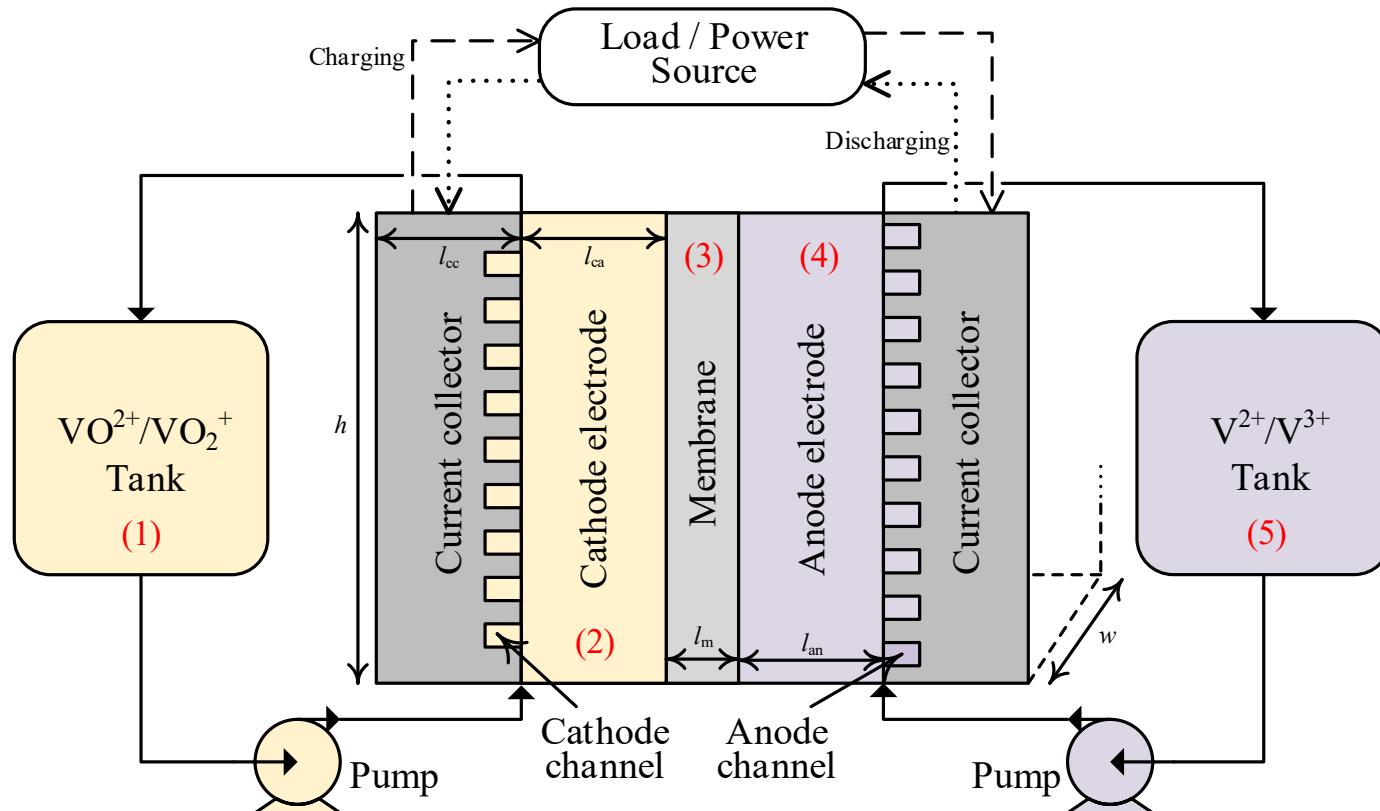
- Fast hydrogen kinetics
- Absence of cross-mixing
- Precious metal catalyst – HOR/HER
- Expertise on PEMFCs



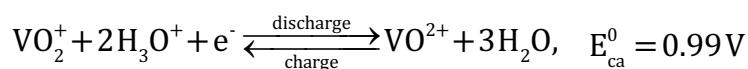
- *Carbon nanotube electrode*
- *NR 212*
- *SGL 35 BC GDL, 0.48 mg Pt cm⁻²*



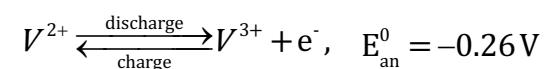
Unit cell model for the VRFB

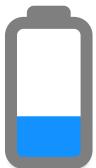


Cathode:



Anode:



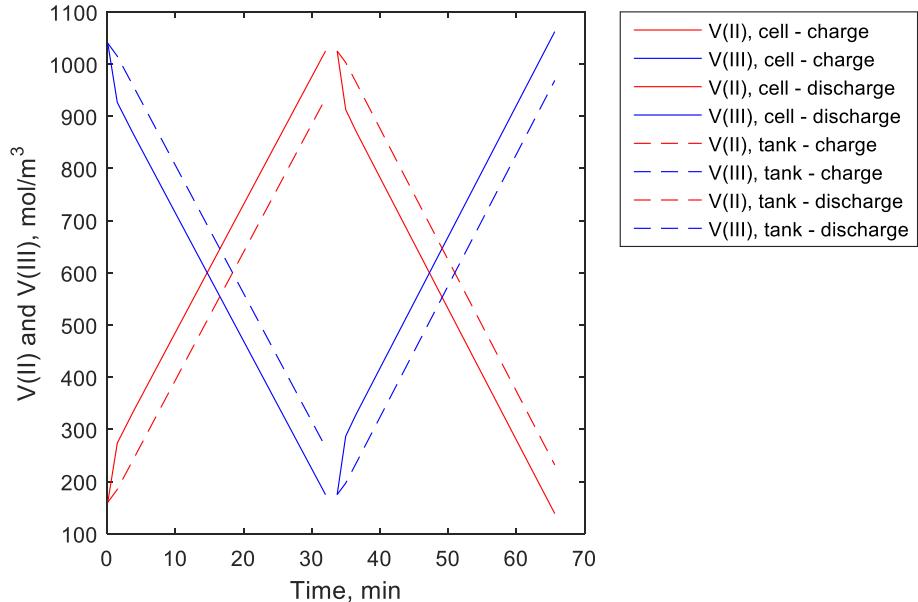


Model summary

Mass conservation

Equilibrium potential

Electrochemical kinetics



Anode

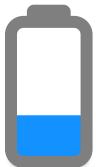
$$j_{\text{an}}^{\text{BV}} = j_{0,\text{an}}^{\text{BV}} \left[\left(\frac{c_{\text{V}^{2+}}^s}{c_{\text{V}^{2+}}^b} \right) \exp \left(\frac{-\alpha F \eta_{\text{an}}}{RT} \right) - \left(\frac{c_{\text{V}^{3+}}^s}{c_{\text{V}^{3+}}^b} \right) \exp \left(\frac{(1-\alpha) F \eta_{\text{ca}}}{RT} \right) \right]$$

Cathode

$$j_{\text{ca}}^{\text{BV}} = j_{0,\text{ca}}^{\text{BV}} \left[\left(\frac{c_{\text{VO}_2^+}^s}{c_{\text{VO}_2^+}^b} \right) \left(\frac{c_{\text{H}^+}^s}{c_{\text{H}^+}^b} \right)^2 \exp \left(\frac{-\alpha F \eta_{\text{ca}}}{RT} \right) - \left(\frac{c_{\text{VO}^{2+}}^s}{c_{\text{VO}^{2+}}^b} \right) \exp \left(\frac{(1-\alpha) F \eta_{\text{ca}}}{RT} \right) \right]$$

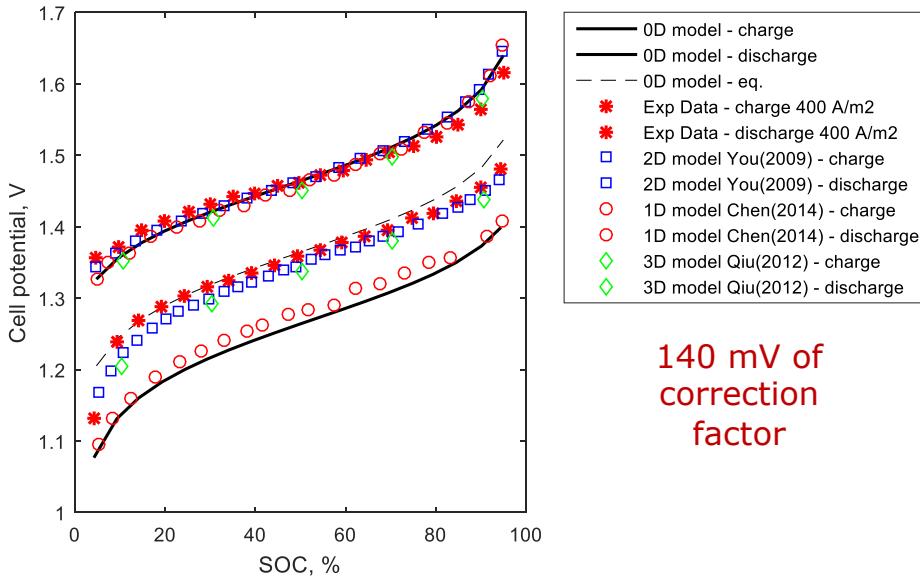
Cell

$$E_{\text{eq}} = E_{\text{cell}}^0 + \frac{RT}{F} \ln \left(\frac{c_{\text{VO}_2^+}^{\text{ca}} \left(c_{\text{H}^+}^{\text{ca}} \right)^2 c_{\text{V}^{2+}}^{\text{an}} \frac{c_{\text{H}^+}^{\text{an}}}{c_{\text{H}^+}^{\text{ca}}} F_\gamma}{c_{\text{VO}^{2+}}^{\text{ca}} c_{\text{V}^{3+}}^{\text{an}} \frac{c_{\text{ca}}^{\text{ca}}}{c_{\text{ca}}^{\text{an}}}} \right)$$

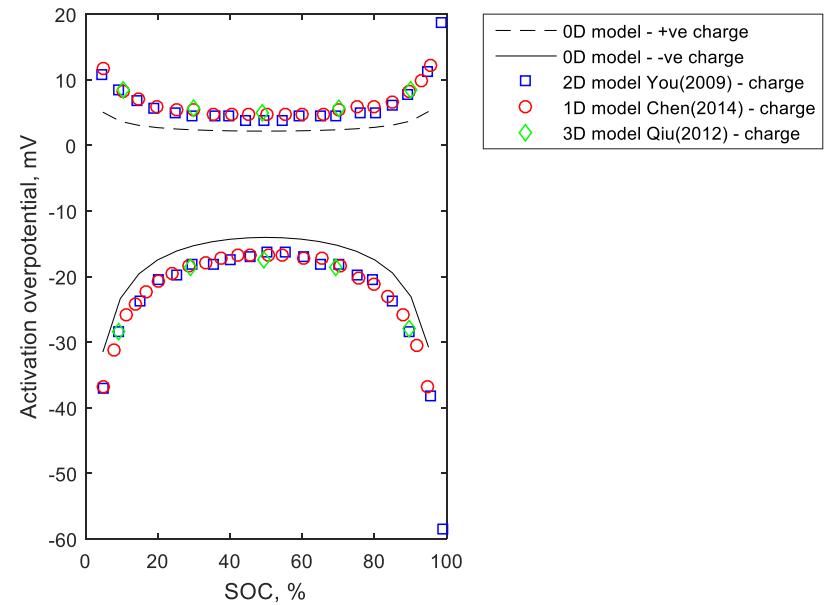


Model validation with literature data

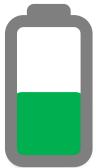
Charge – discharge potential



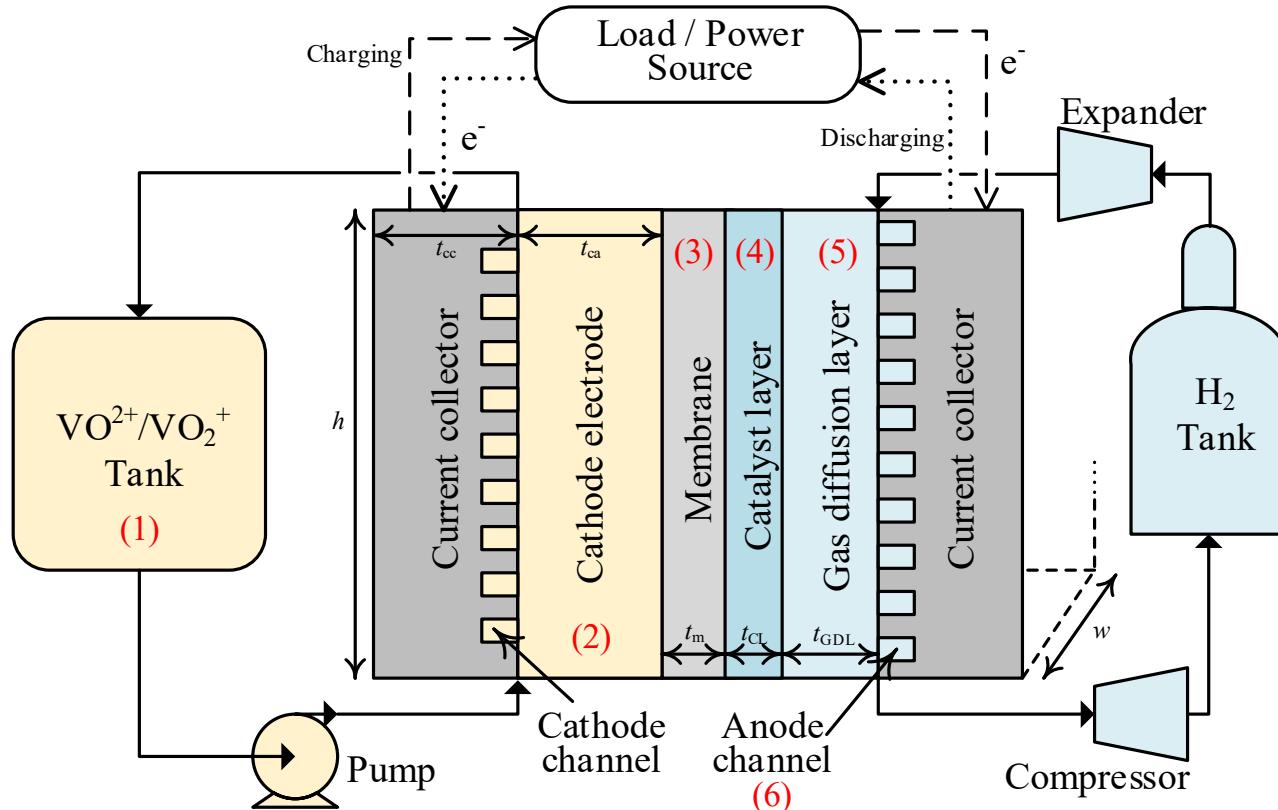
Overpotential



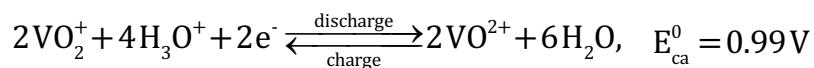
$$c_V = 1500 \text{ mol m}^{-3}, c_{acid} = 5000 \text{ mol m}^{-3}, V = 30 \text{ mL}, j = 400 \text{ A m}^{-2}, Q_V = 60 \text{ mL min}^{-1}$$



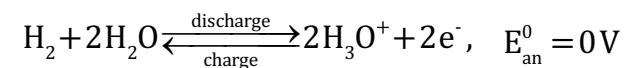
Unit cell model for the RHVFC



Cathode:

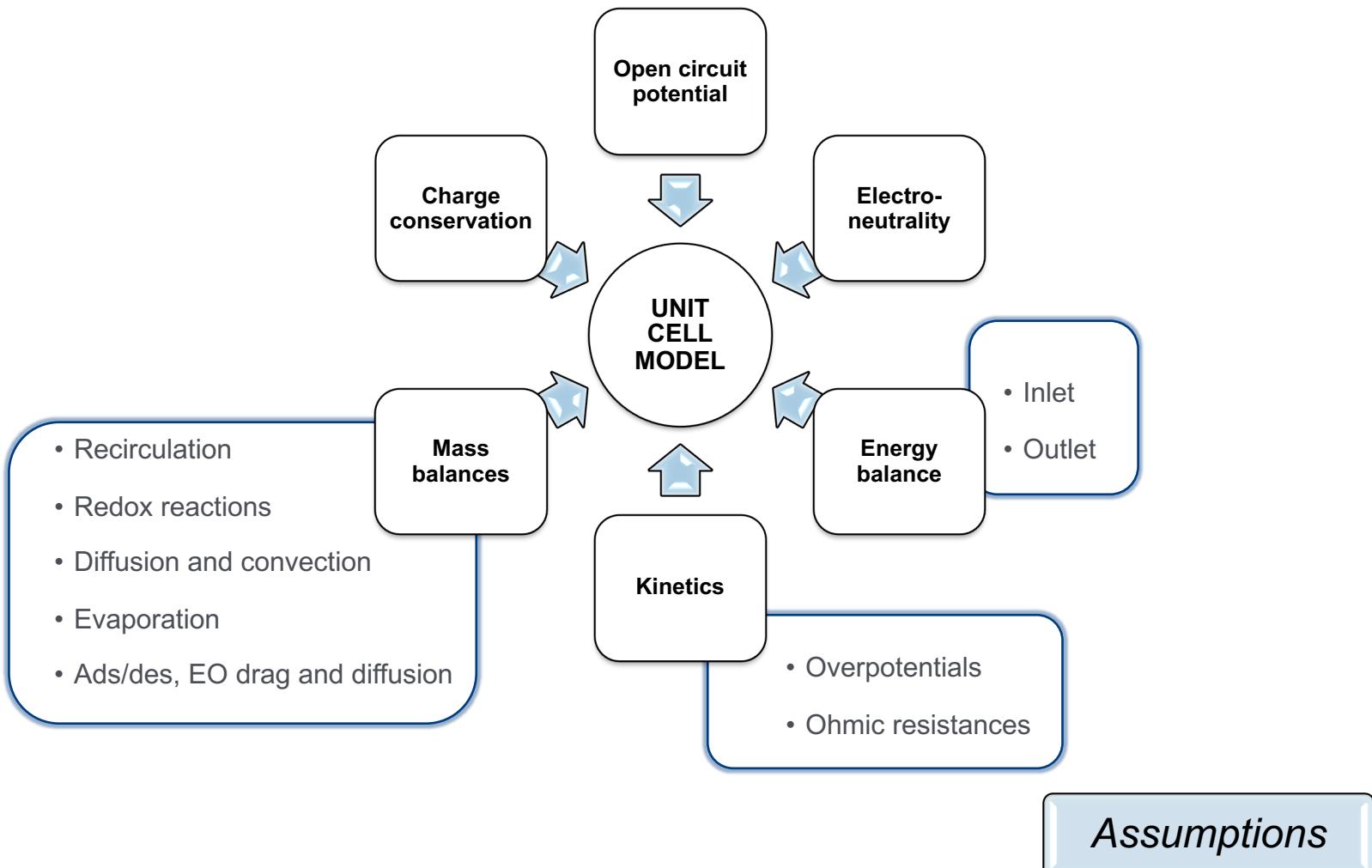


Anode:

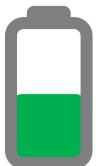




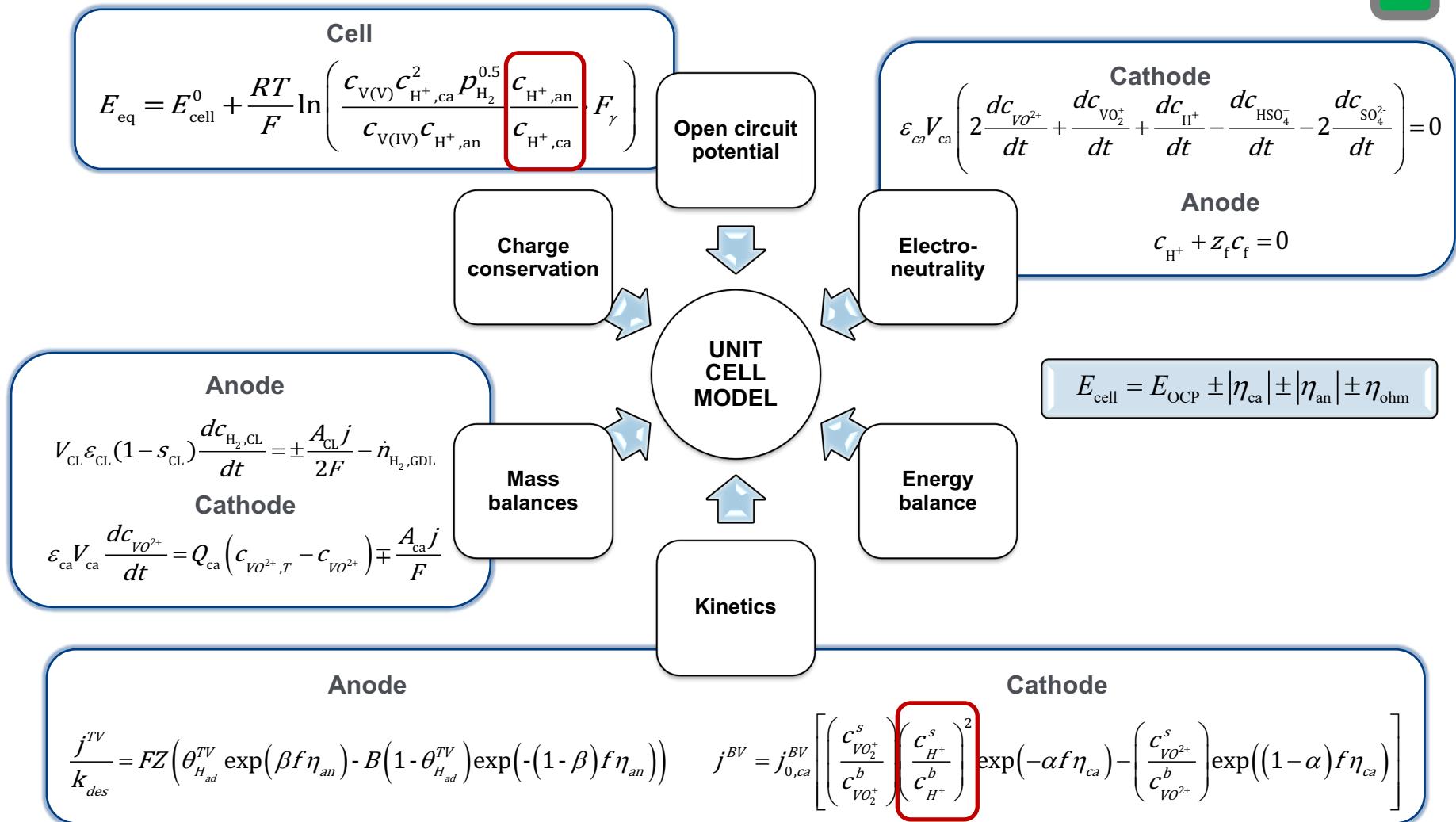
Model summary

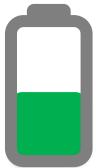


Assumptions



Model summary



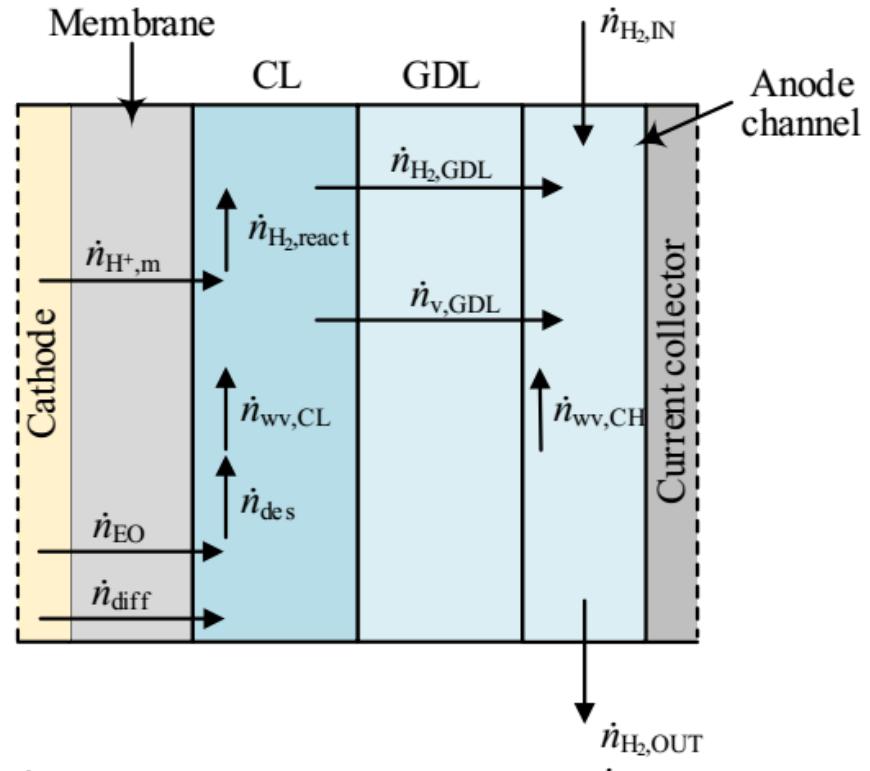


Hydrogen side

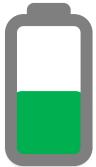
Dissolved water transport

Dusty Gas Model

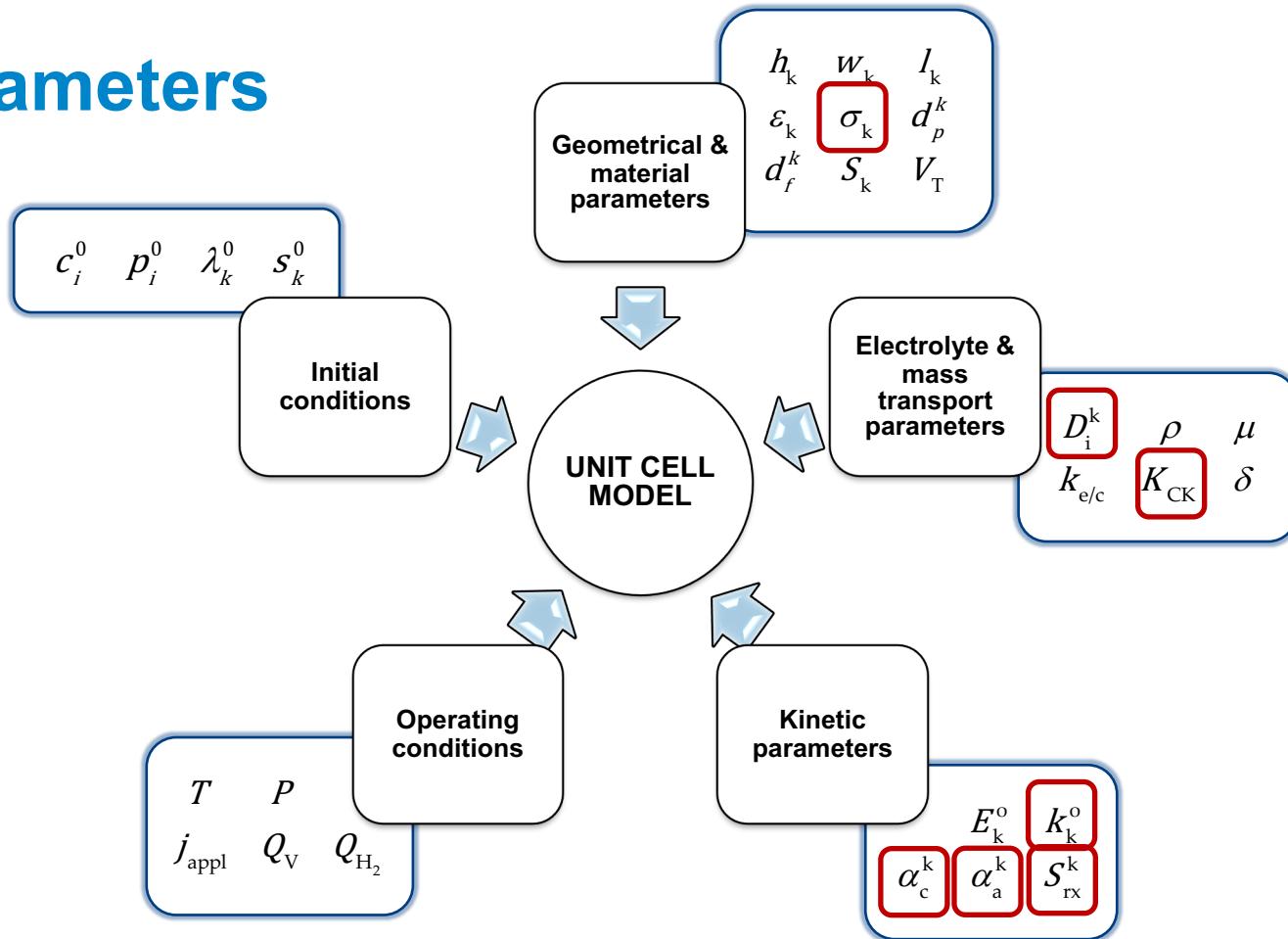
Evaporation/condensation

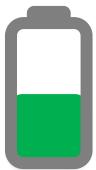


Charge operation

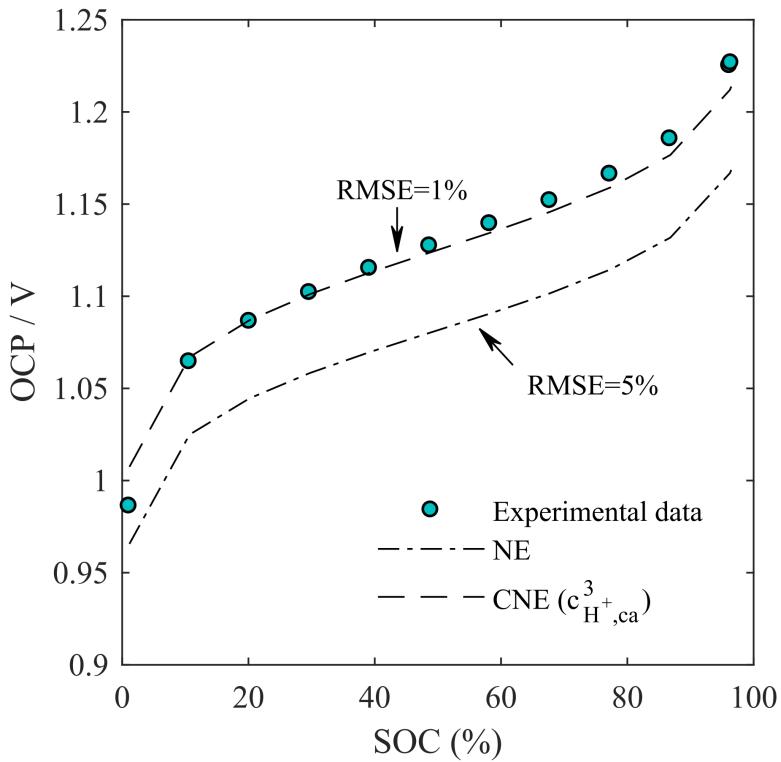


Parameters





Open Circuit Potential



Nernst Equation (NE)

$$E_{OCP} = E_{cell}^0 + \frac{RT}{F} \ln \left(\frac{c_{V(V)} c_{H^{+},ca}^2 p_{H_2}^{0.5}}{c_{V(IV)} c_{H^{+},an}} \right)$$

Complete Nernst Equation (CNE)

$$E_{OCP} = E_{cell}^0 + \frac{RT}{F} \ln \left(\frac{c_{V(V)} c_{H^{+},ca}^2 p_{H_2}^{0.5} c_{H^{+},ca}}{c_{V(IV)} c_{H^{+},an} c_{H^{+},an}} \right)$$

*Donnan potential
across the membrane
(dialysis potential)*

→ $E_m = \frac{RT}{F} \ln \left(\frac{c_{H^{+},ca}}{c_{H^{+},an}} \right)$

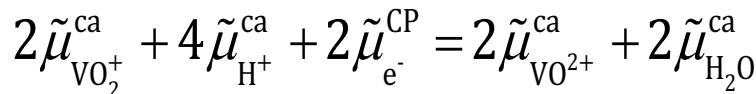
*Inconsistent with
thermodynamics*

$$\tilde{\mu}_i = \mu_i + z_i F \phi$$

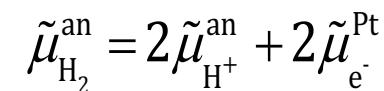


*Electrochemical potential
of species i*

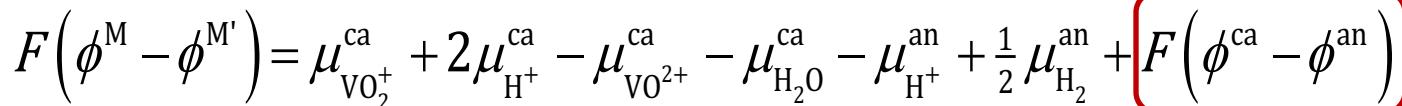
Equilibrium



Cathode reaction



Anode reaction



Cell



*Donnan potential
across both interfaces
(dialysis potential)*



$$FE_{\text{Don}}^m = F(\phi^{ca} - \phi^{an}) = \mu_{H^+}^{an} - \mu_{H^+}^{ca}$$



$$\mu_i = \mu_i^0 + RT \ln(a_i)$$

$$a_i = \gamma_i c_i$$

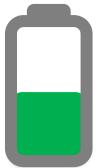
*Chemical potential of
species *i**

Equilibrium

$$E_{OCP} = E_{cell}^0 + \frac{RT}{F} \ln \left(\frac{a_{V0_2^+}^{ca} (a_{H^+}^{ca})^2 (a_{H_2}^{an})^{0.5}}{a_{V0^{2+}}^{ca} a_{H_2O}^{ca} a_{H^+}^{an}} \times \frac{a_{H^+}^{an}}{a_{H^+}^{ca}} \right)$$

*Thermodynamic
derivation*

*Potential difference
between electrolytes*



Complete Nernst Equation

$$E_{OCP} = E_{\text{cell}}^0 + \frac{RT}{F} \ln \left(\frac{c_{\text{VO}_2^+}^{\text{ca}} \left(c_{\text{H}^+}^{\text{ca}} \right)^2 \left(p_{\text{H}_2}^{\text{g}} \right)^{0.5}}{c_{\text{VO}^{2+}}^{\text{ca}} c_{\text{H}^+}^{\text{an}}} \times \frac{c_{\text{H}^+}^{\text{an}}}{c_{\text{H}^+}^{\text{ca}}} \times \frac{\gamma_{\text{VO}_2^+}^{\text{ca}} \gamma_{\text{H}^+}^{\text{ca}}}{\gamma_{\text{VO}^{2+}}^{\text{ca}}} \right)$$

Nernst equation
↑
↑
↓

*Thermodynamic
derivation*

*Potential difference
between electrolytes*

$$\phi^{\text{ca}} - \phi^{\text{an}} = \frac{RT}{F} \ln \left(\frac{c_{\text{H}^+}^{\text{an}}}{c_{\text{H}^+}^{\text{ca}}} \right)$$



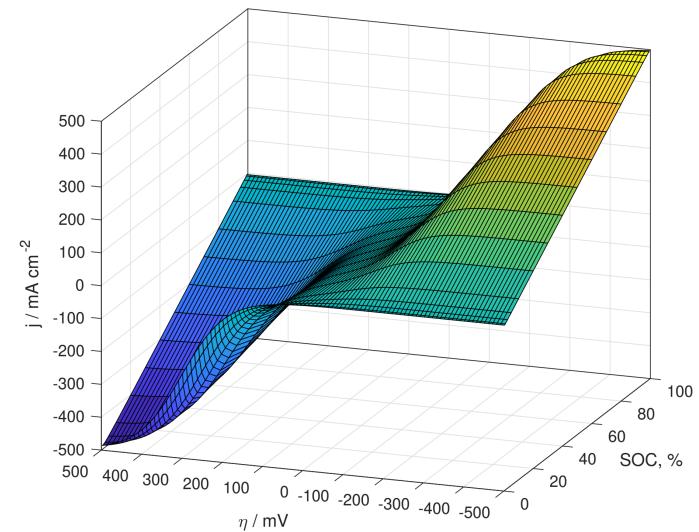
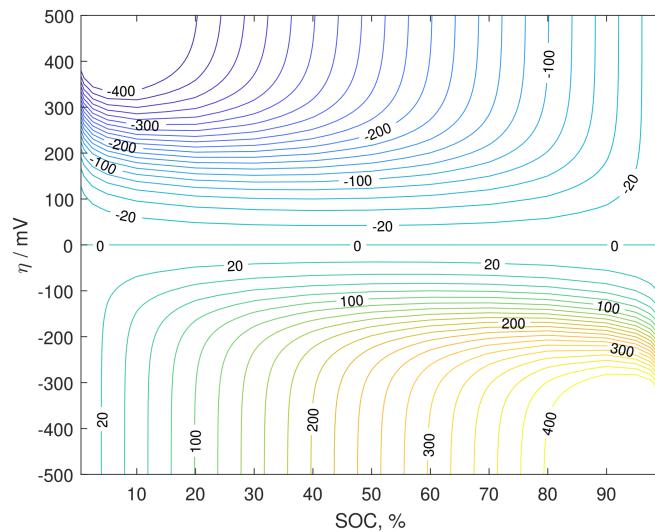
Complete Butler-Volmer equation for cathode

$$j^{BV} = j_{0,ca}^{BV} \left[\left(\frac{c_{VO^{2+}}^s}{c_{VO^{2+}}^b} \right) \exp \left(\frac{\alpha_a F \eta_{ca}}{RT} \right) - \left(\frac{c_{VO_2^+}^s}{c_{VO_2^+}^b} \right) \left(\frac{c_{H^+}^s}{c_{H^+}^b} \right)^2 \exp \left(\frac{-\alpha_c F \eta_{ca}}{RT} \right) \right]$$



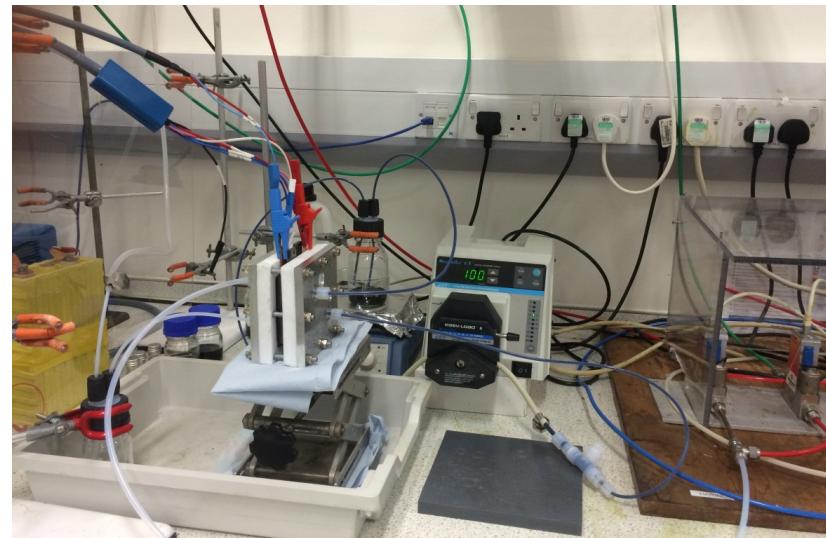
$$j_{0,ca}^{BV} = F k_{ca} \left(c_{VO^{2+}}^b \right)^{\alpha_c} \left(c_{VO_2^+}^b \right)^{\alpha_a} \left(c_{H^+}^b \right)^{2\alpha_a}$$

Protons concentration

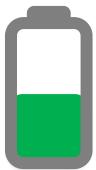




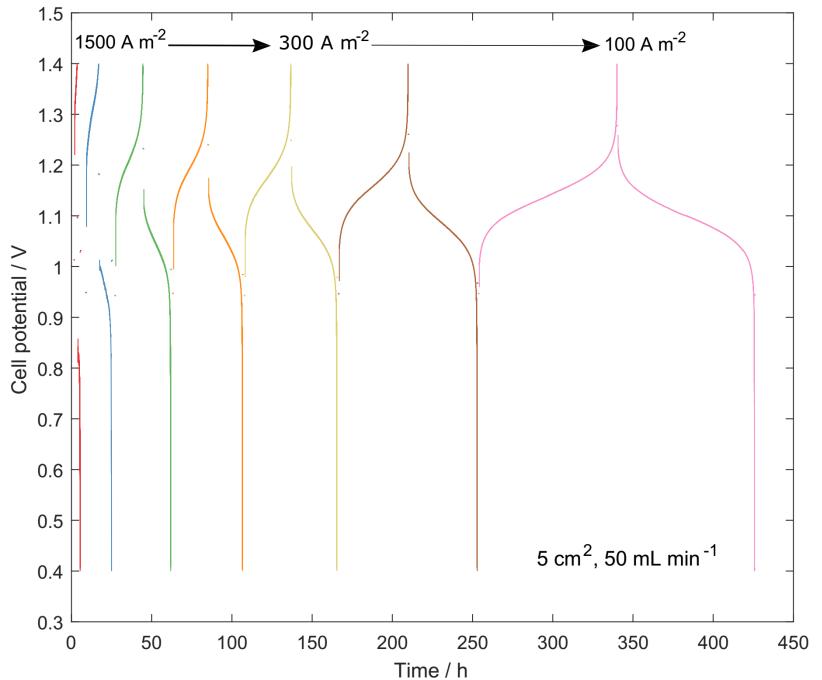
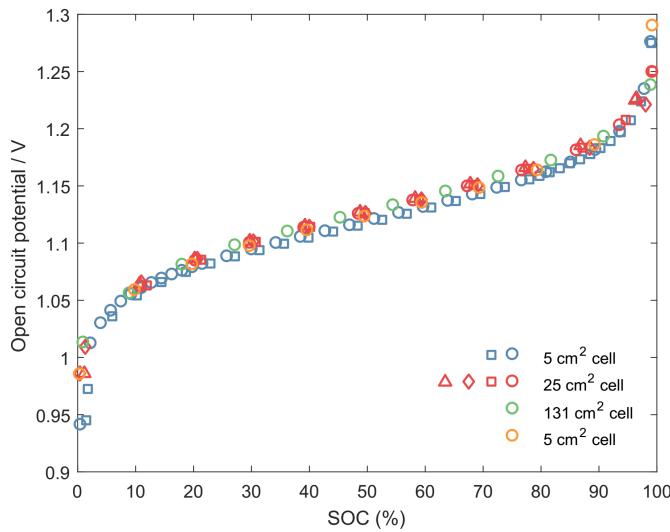
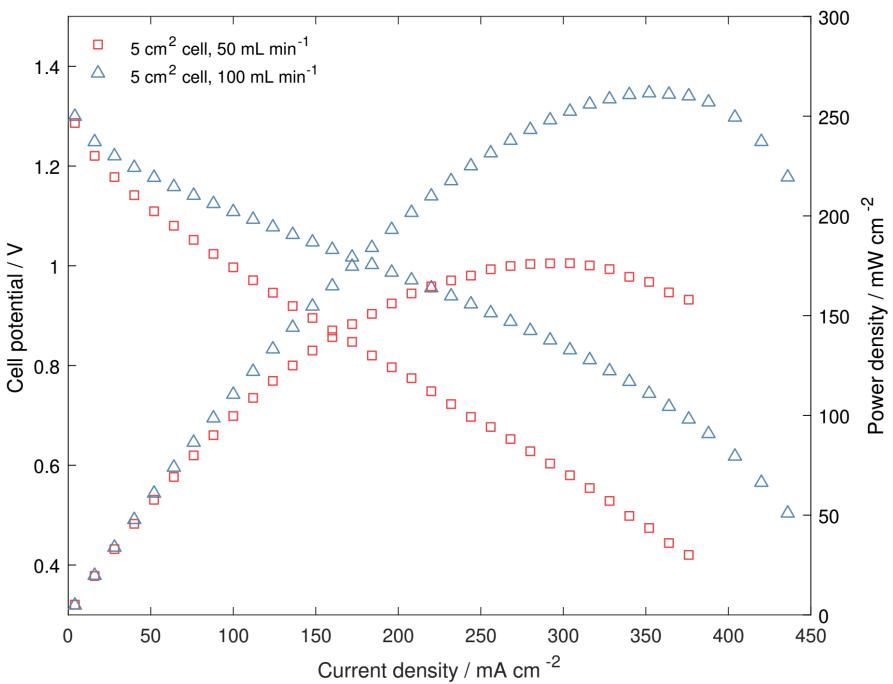
Experimental data RHVFC



Cell	1	2	3
Area	25 cm ²	5 cm ²	5 cm ²
Cathode	SGL 10AA, 400 µm, untreated	SGL 10AA, 400 µm, untreated	Freudenberg H23, 210 µm, heat treated (500 °C, 6 h)
Anode	Alfa Aesar, 200 µm, 0.5 mg cm ⁻² Pt	SGL 25BC, 235 µm, 0.2 mg cm ⁻² Pt	SGL 29BC, 235 µm, 0.3 mg cm ⁻² Pt
Membrane	Nafion 117, 183 µm	Nafion 117, 183 µm	Nafion 115, 127 µm
Flow channel	Multi-channel serpentine	Single-channel serpentine	Single-channel serpentine
Catholyte	1M VOSO ₄ in 60 mL 5M H ₂ SO ₄	1M VOSO ₄ in 60 mL 5M H ₂ SO ₄	0.75M VOSO ₄ in 60 mL 5M H ₂ SO ₄
Current density	50 – 600 A m ⁻²	1000 & 2000 A m ⁻²	500 – 1500 A m ⁻²
Catholyte flow rate	100 & 150 mL min ⁻¹	77 mL min ⁻¹	50 & 100 mL min ⁻¹
Hydrogen flow rate	50 & 100 mL min ⁻¹	100 mL min ⁻¹	100 mL min ⁻¹
Tests	OCP, ch-dch, polarization	dch, polarization, RE	OCP, ch-dch, polarization

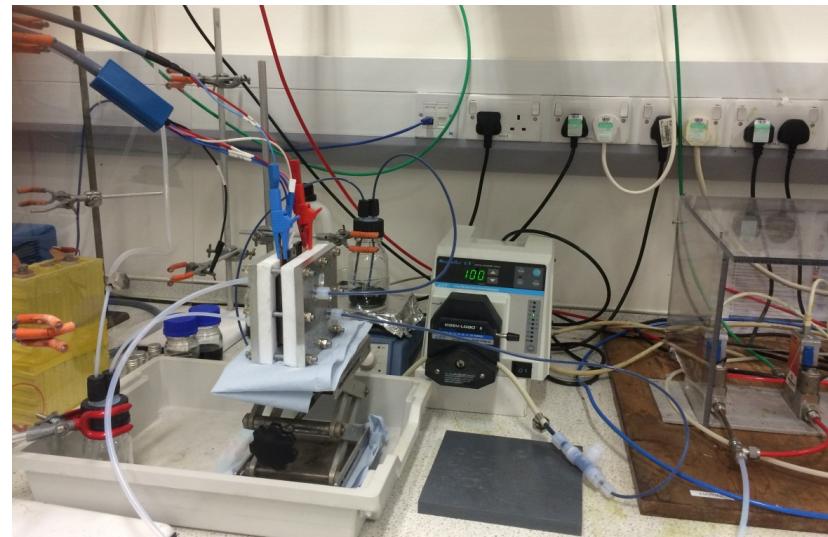


Experimental data RHVFC



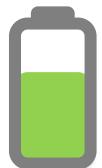


Experimental data RHVFC



Cell 3	AVIZO	TauFactor
Area	5 cm ²	
Cathode	Freudenberg H23, 210 µm, heat treated (500 °C, 6 h)	
Porosity	0.848	0.850
Specific surface area	68.9 µm ² µm ⁻³	73.8 µm ² µm ⁻³
Mean pore diameter	31.77 µm	---
Mean fibre diameter	13.50 µm	---

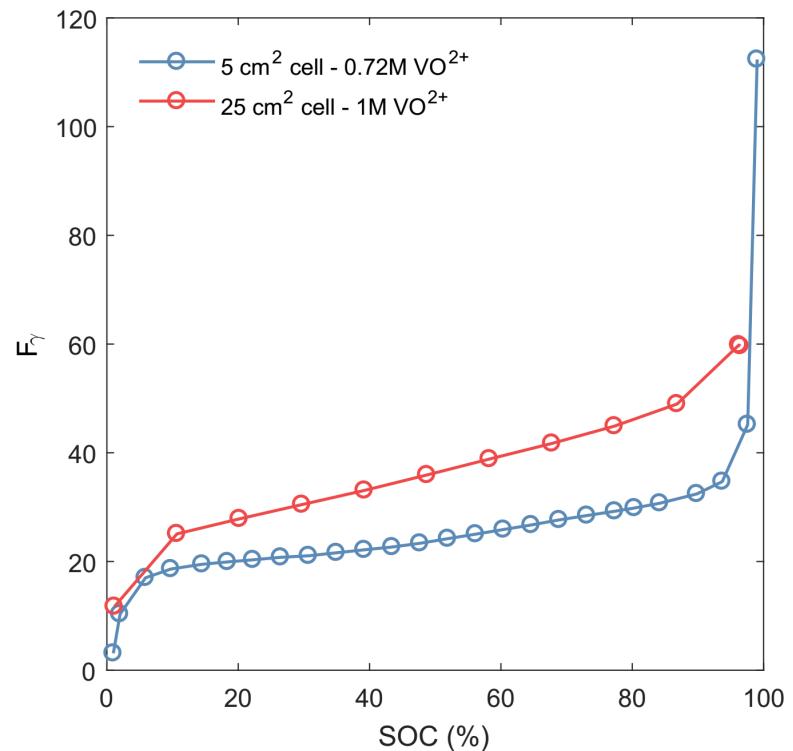
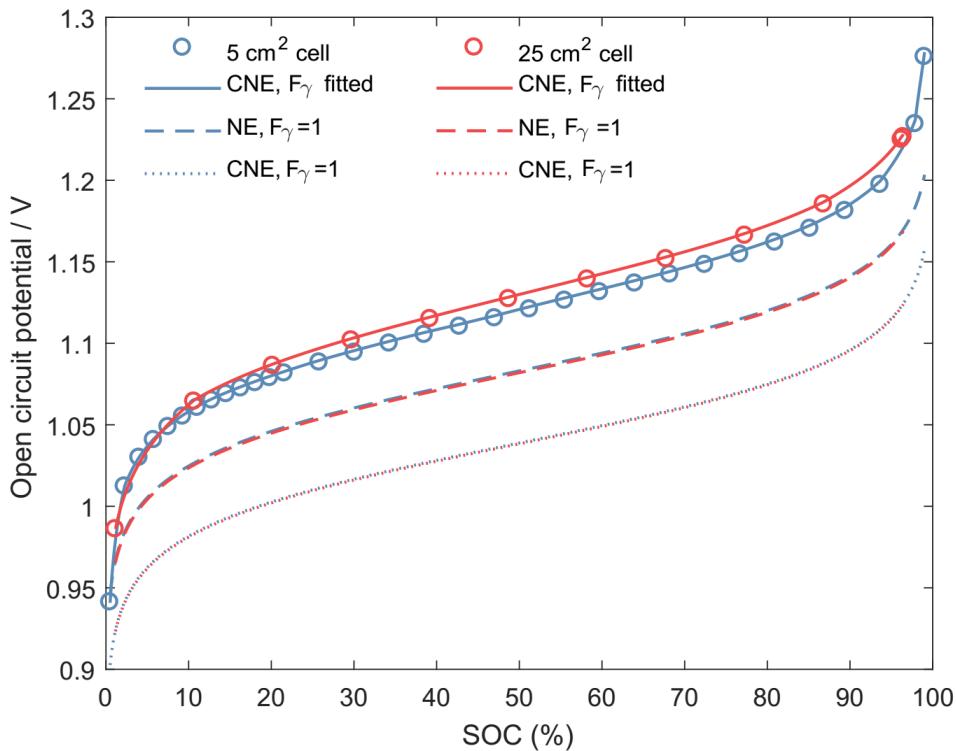


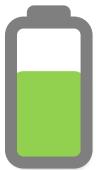


Open Circuit Potential

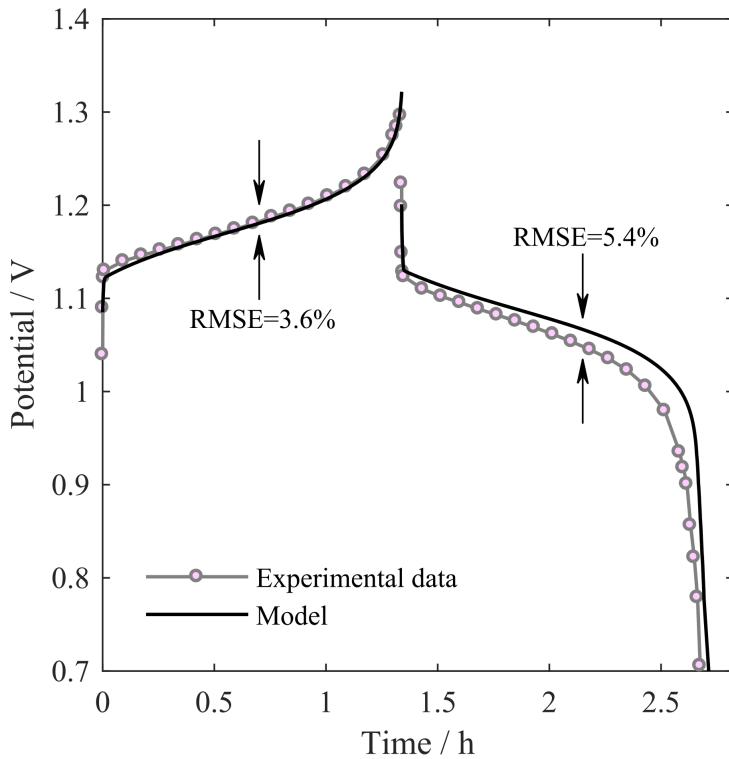
Thermodynamic derivation of CNE

$$E_{OCP} = E_{cell}^0 + \frac{RT}{F} \ln \left(\frac{c_{VO_2^{+}}^{ca} (c_{H^+}^{ca})^2 (p_{H_2}^g)^{0.5}}{c_{VO^{2+}}^{ca} c_{H^+}^{an}} \times \frac{c_{H^+}^{an}}{c_{H^+}^{ca}} \times F_\gamma \right)$$





Model calibration



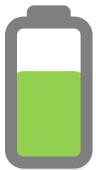
Model implementation

- MATLAB
- ode15s → solve ODE problem
- lsqcurvefit → curve fitting, lb & ub

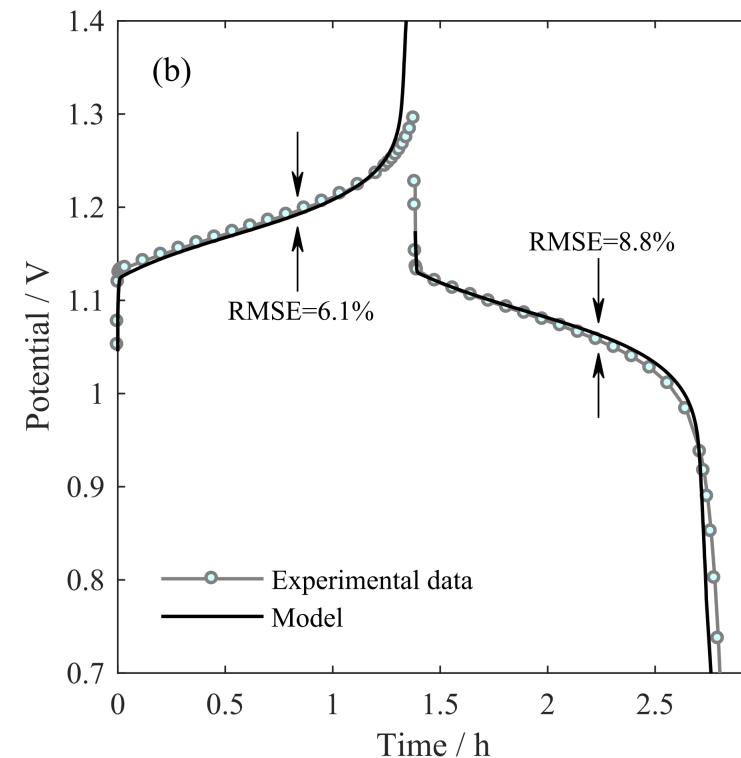
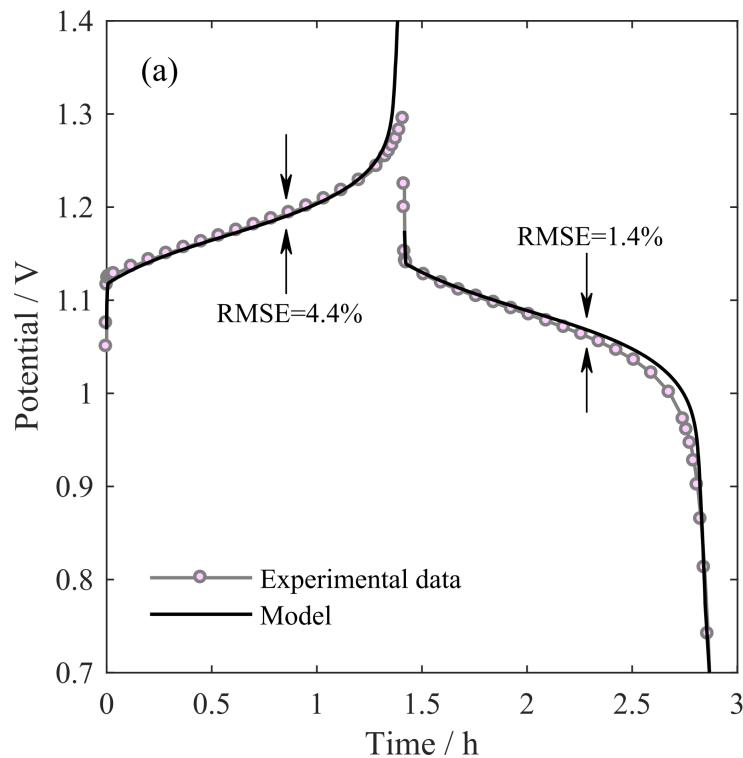
Fitting parameters

- Standard rate constant of cathode → k_{ca}^0
- Nernst diffusion layer thickness → δ
- Additional Ohmic resistance (contact) → R_C

Cell 1: 25 cm^2 , $j = 400 \text{ A m}^{-2}$, $Q_V=Q_{H_2}=100 \text{ mL min}^{-1}$

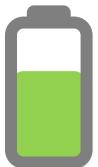


Charge-discharge: vary flow rate

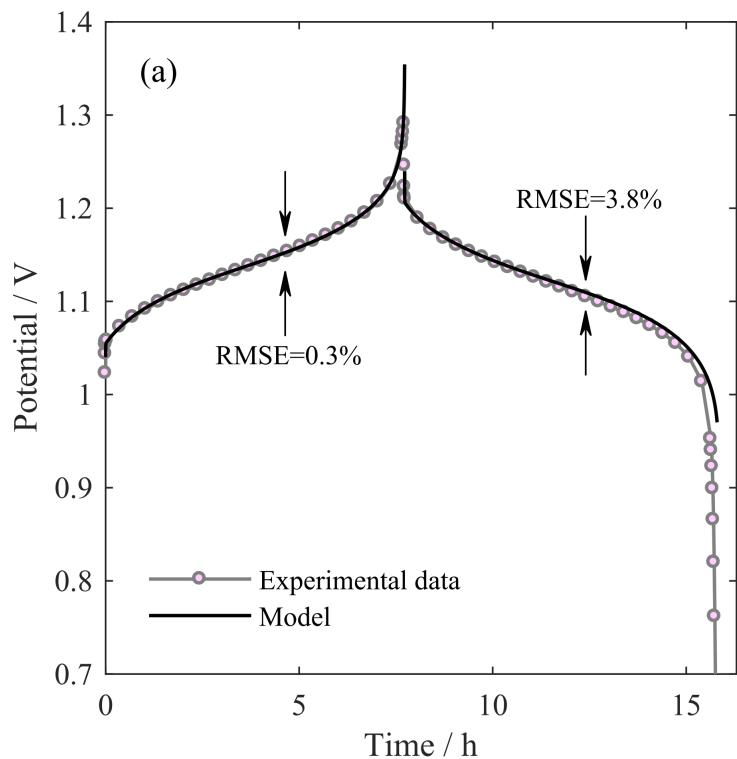


Cell 1: $j = 400 \text{ A m}^{-2}$, $Q_V = 150 \text{ mL min}^{-1}$, $Q_{H_2} = 100 \text{ mL min}^{-1}$

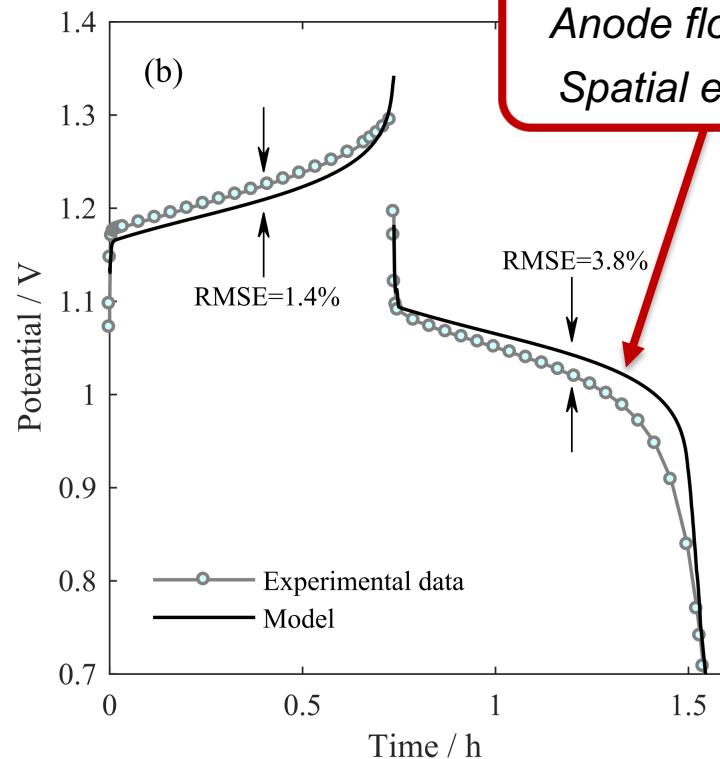
Cell 1: $j = 400 \text{ A m}^{-2}$, $Q_V = 100 \text{ mL min}^{-1}$, $Q_{H_2} = 50 \text{ mL min}^{-1}$



Charge-discharge: vary current density

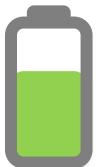


Cell 1: 25 cm^2 , $j = 80 \text{ A m}^{-2}$, $Q_V=Q_{H_2}=100 \text{ mL min}^{-1}$

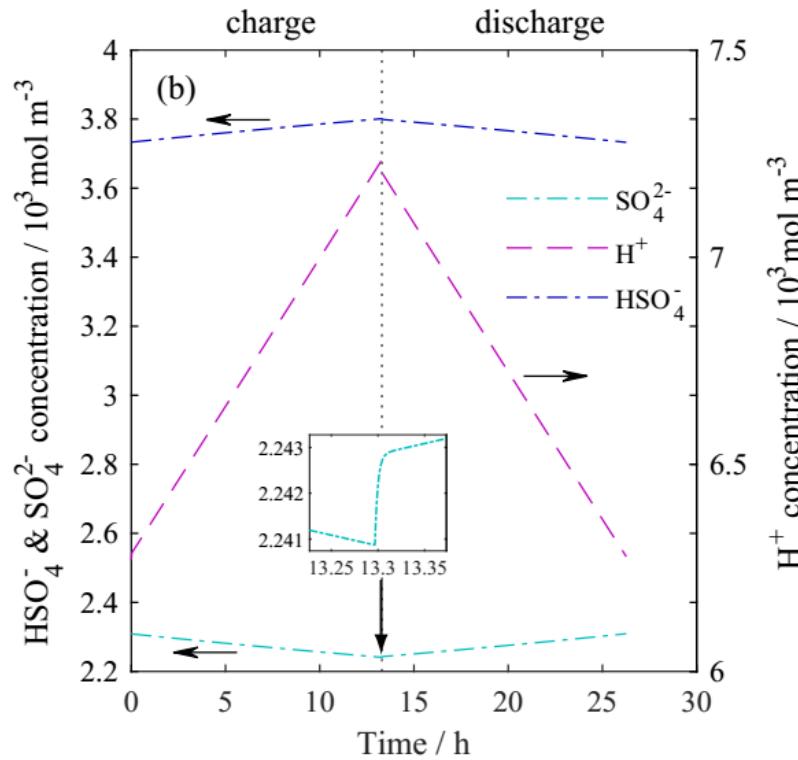
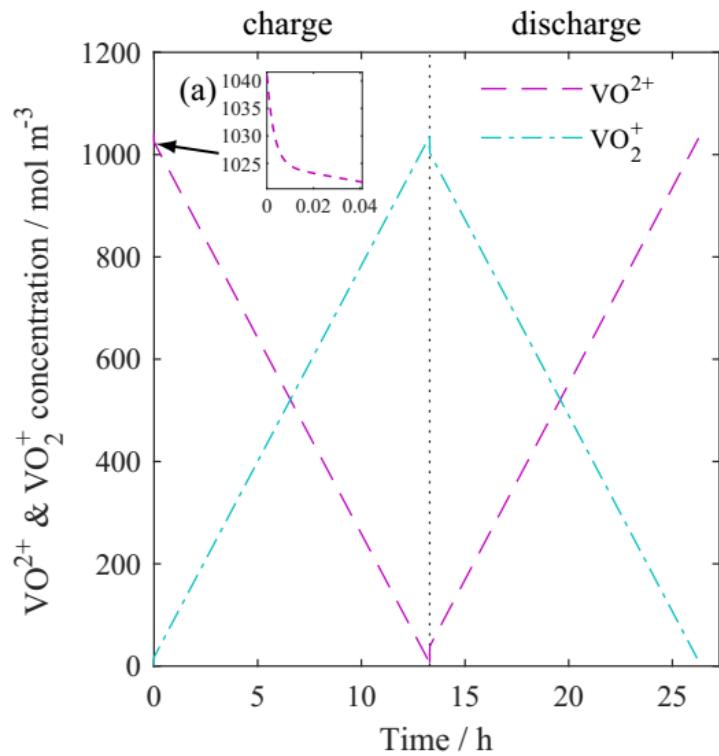


Cell 1: 25 cm^2 , $j = 600 \text{ A m}^{-2}$, $Q_V=Q_{H_2}=100 \text{ mL min}^{-1}$

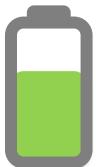
*Bulk diffusion
Crossover
Anode flooding
Spatial effects*



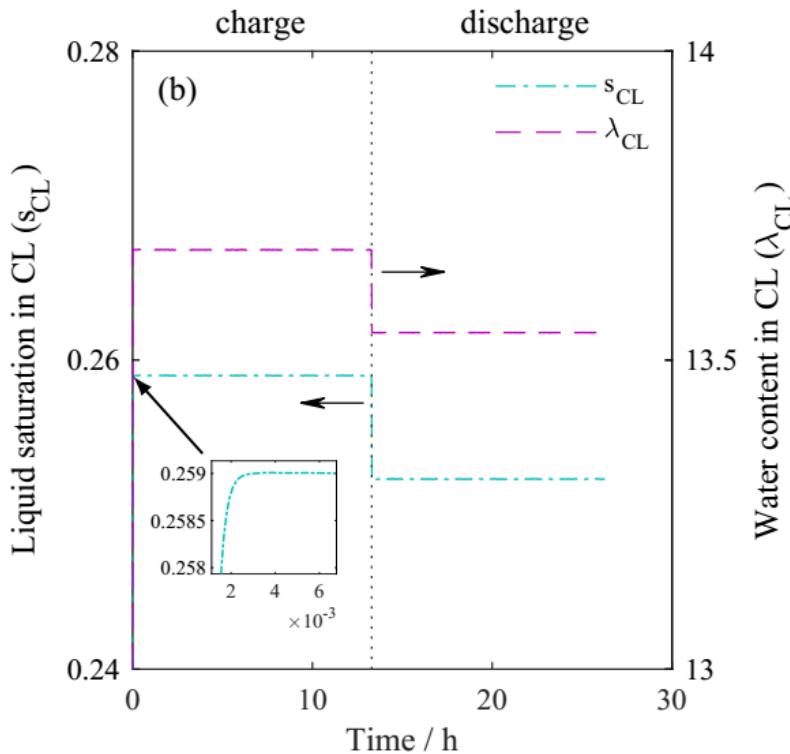
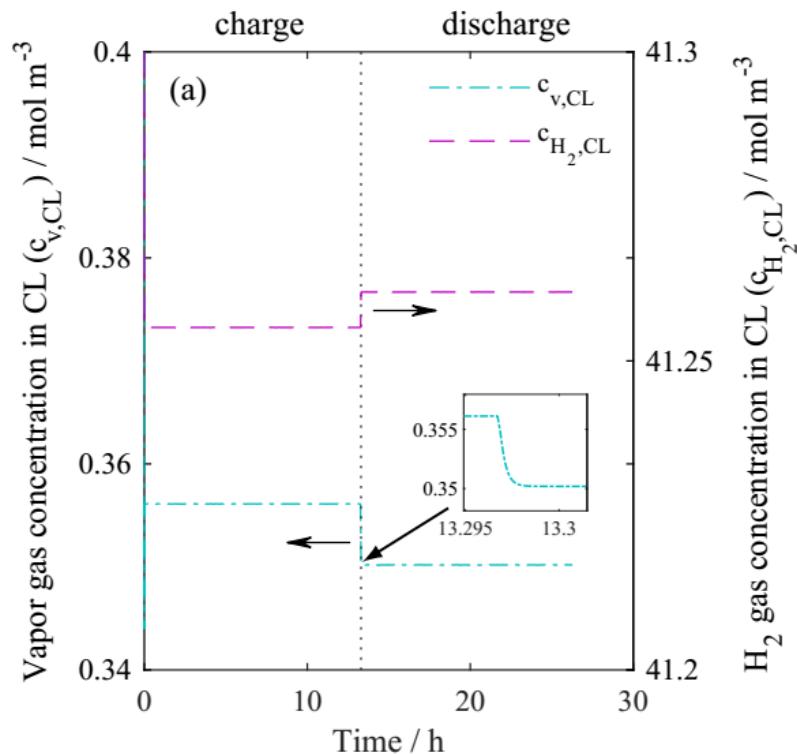
Species evolution in cathode



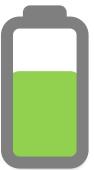
Cell 1: $j = 50 \text{ A m}^{-2}$, $Q_V = Q_{H_2} = 100 \text{ mL min}^{-1}$



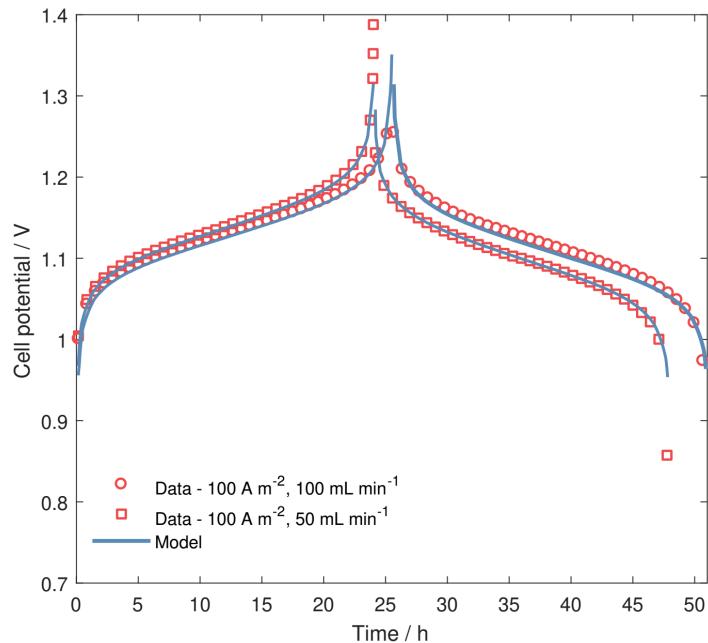
Species evolution in anode



Cell 1: $j = 50 \text{ A m}^{-2}$, $Q_V = Q_{H_2} = 100 \text{ mL min}^{-1}$



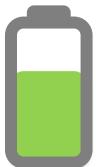
Charge-discharge



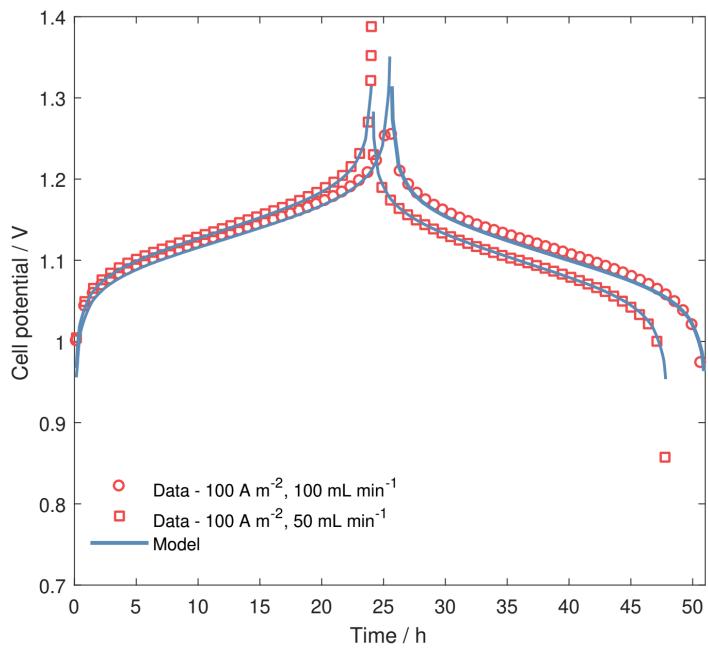
Fitting parameters

- Standard rate constant of cathode $\rightarrow k_{\text{ca}}^0$
- Specific surface (active) area of cathode $\rightarrow S_{\text{rx}}^{\text{ca}}$
- Standard desorption rate constant of anode $\rightarrow k_{\text{des}}^0$
- Electronic conductivity of current collectors $\rightarrow \sigma^{\text{cc}}$

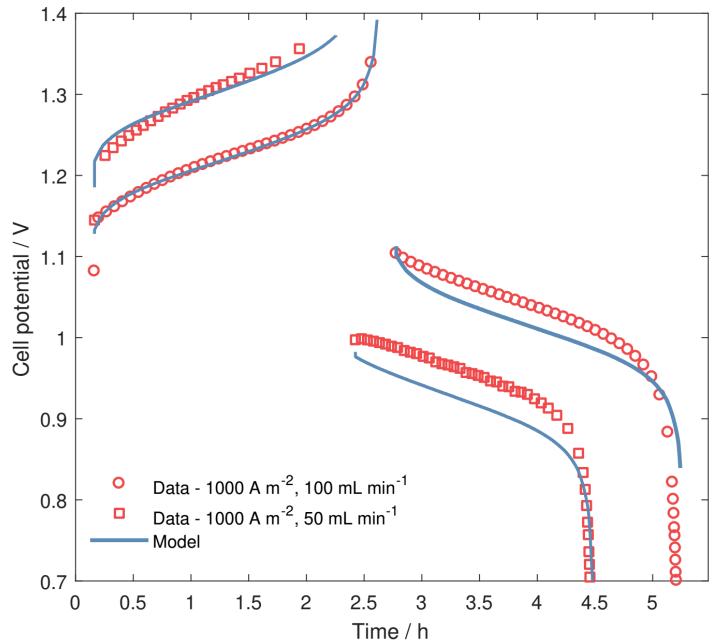
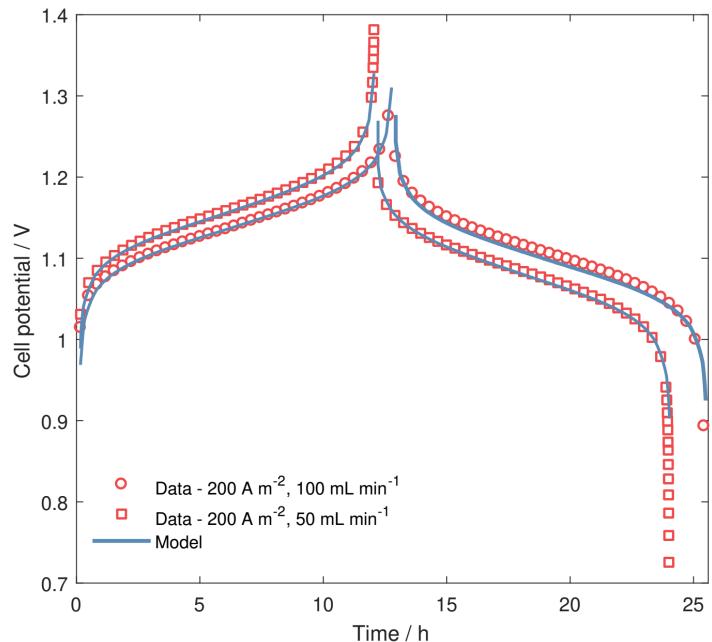
Cell 3: $Q_V=50 \text{ & } 100 \text{ mL min}^{-1}$, $Q_{H_2}=100 \text{ mL min}^{-1}$

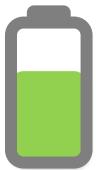


Charge-discharge

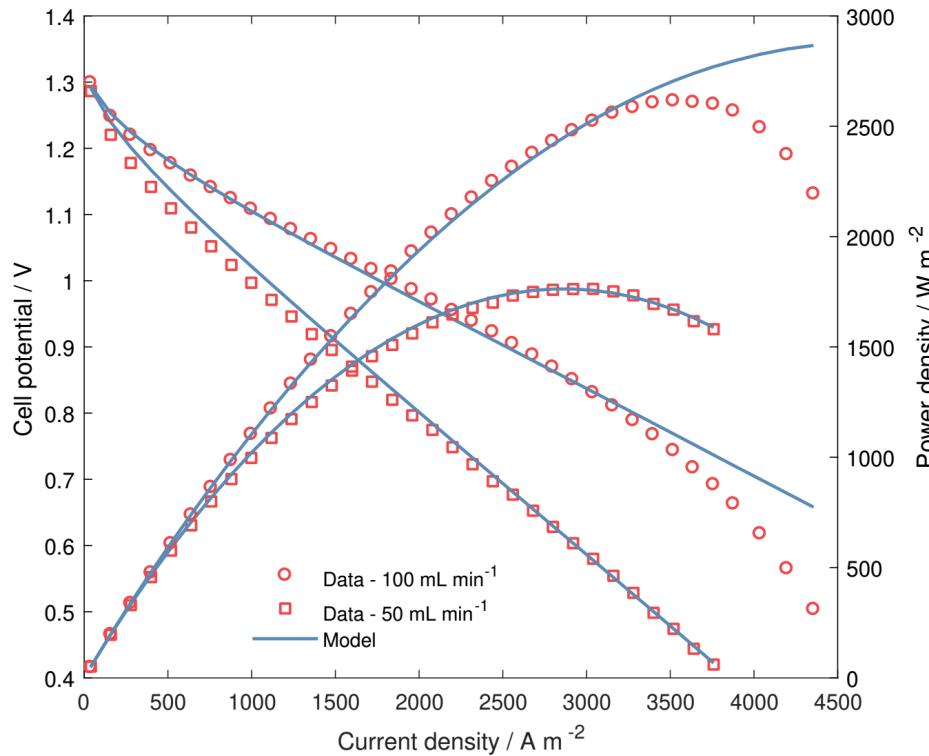


Cell 3: $Q_V=50$ & 100 mL min^{-1} , $Q_{H_2}=100 \text{ mL min}^{-1}$

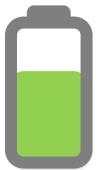




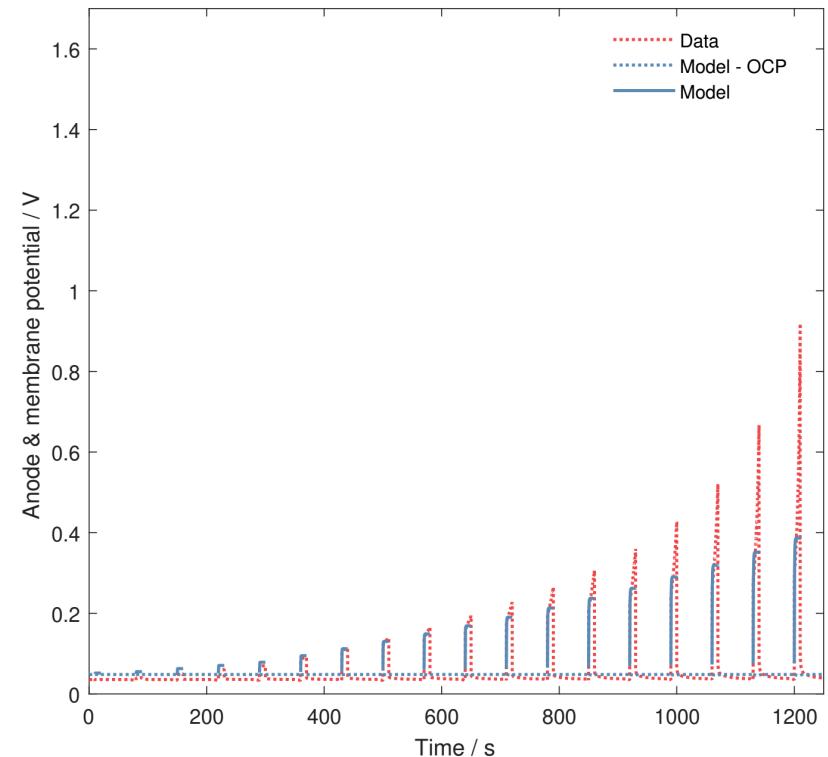
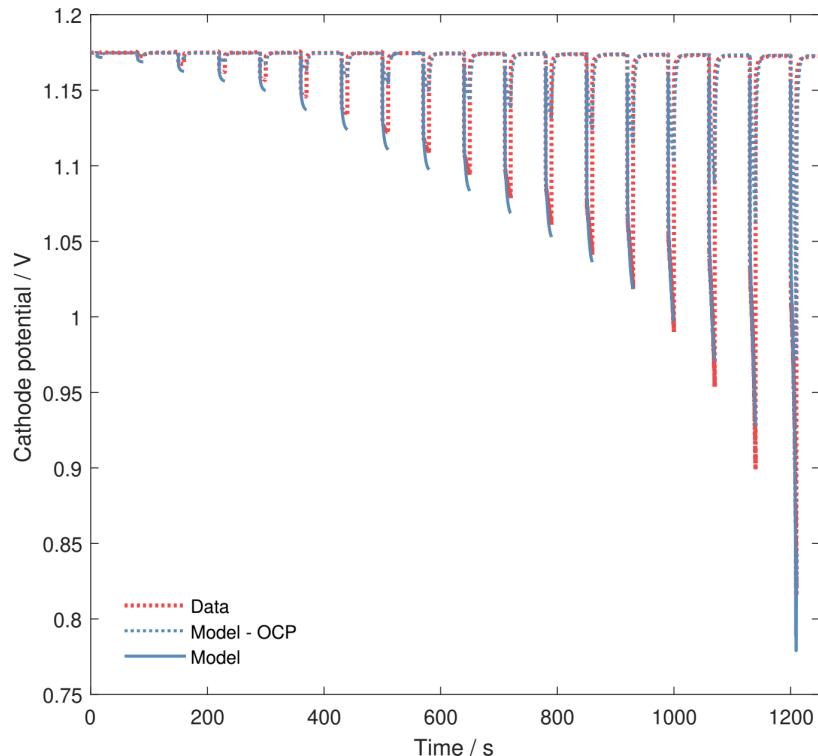
Polarization curve



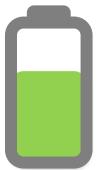
Cell 3: 100% SOC, $Q_V=50$ & 100 mL min^{-1} , $Q_{H_2}=100 \text{ mL min}^{-1}$



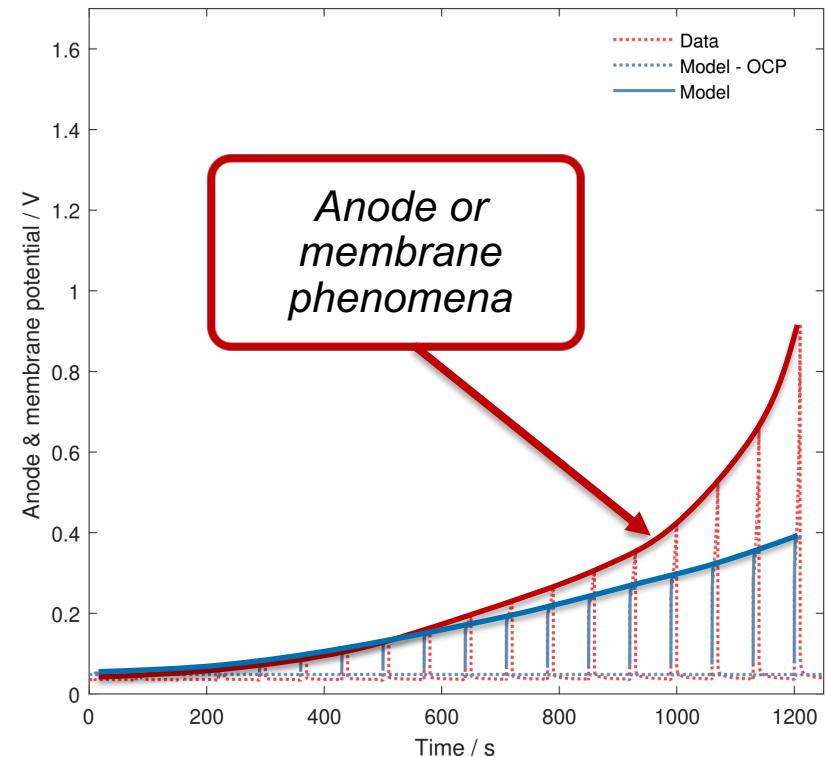
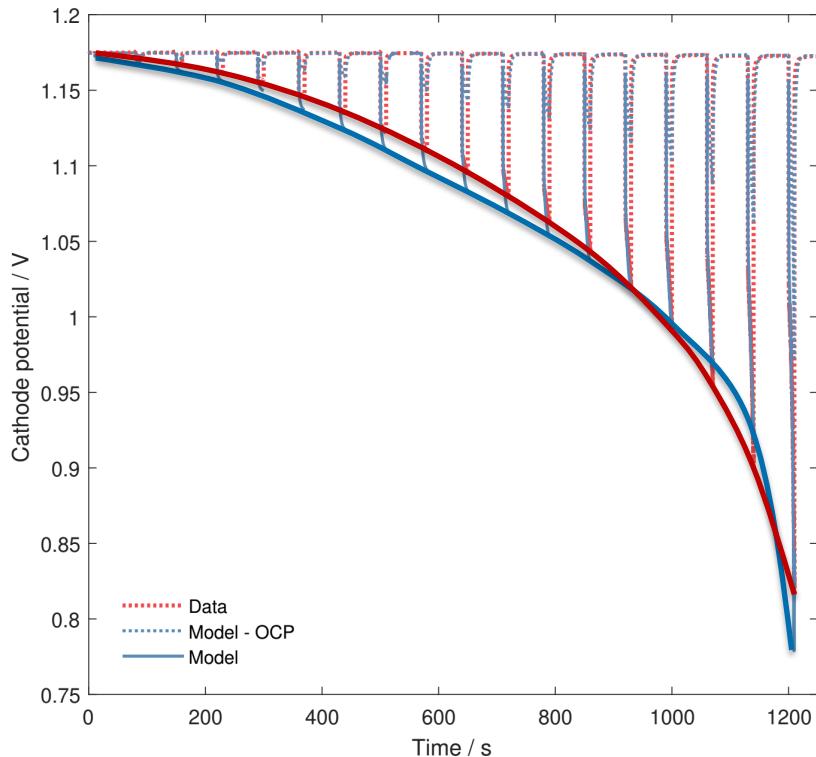
Polarization curves – reference electrodes



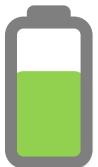
Cell 2: 50% SOC, $Q_V=77 \text{ mL min}^{-1}$, $Q_{H_2}=100 \text{ mL min}^{-1}$



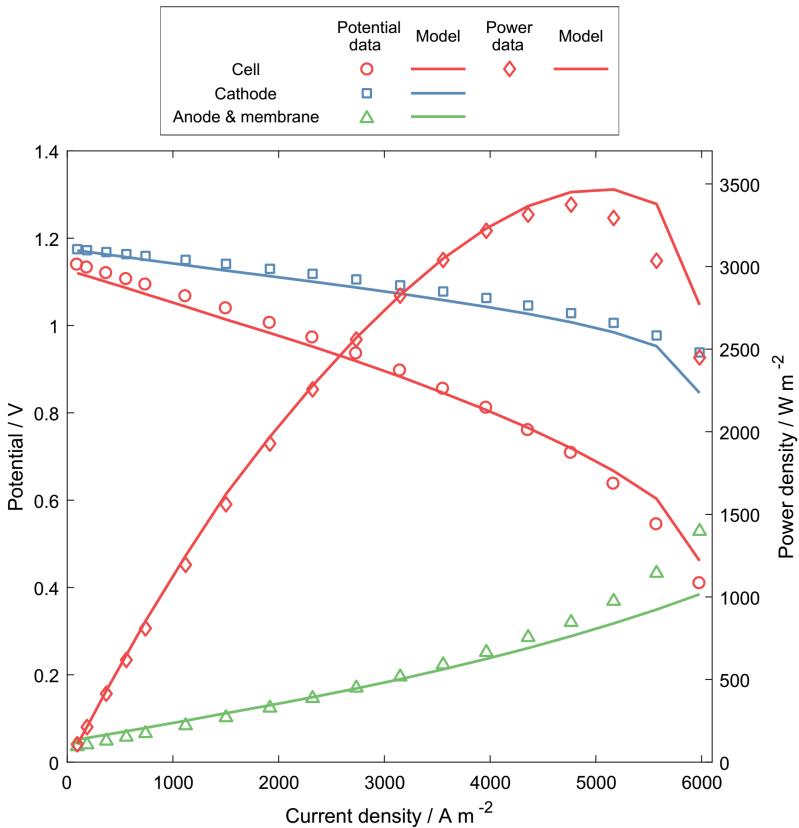
Polarization curves – reference electrodes



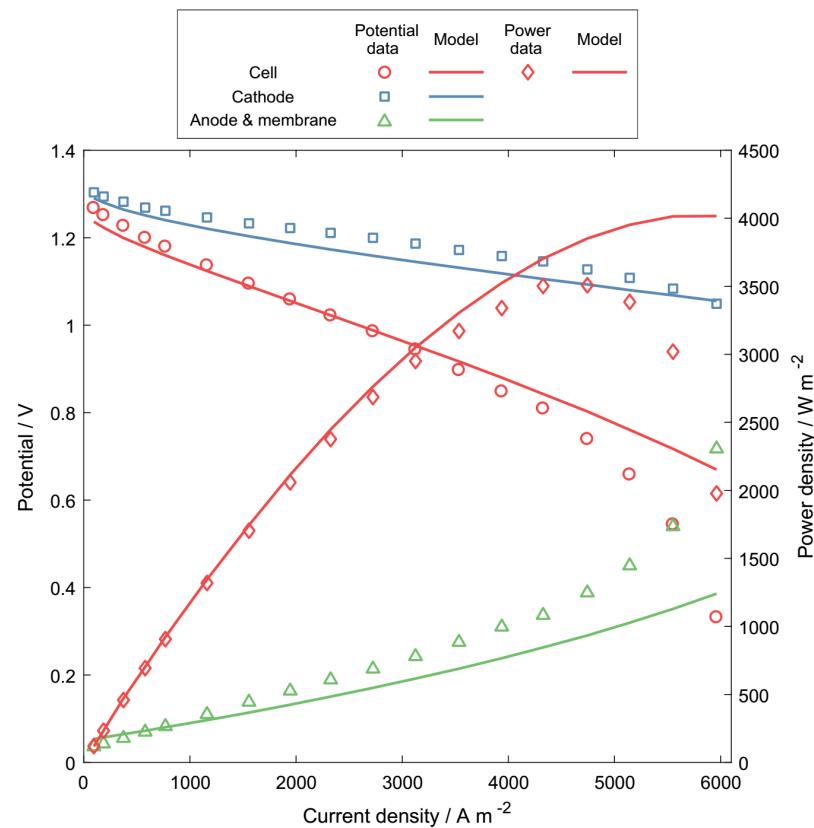
Cell 2: 50% SOC, $Q_V=77 \text{ mL min}^{-1}$, $Q_{H_2}=100 \text{ mL min}^{-1}$



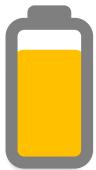
Polarization curves – reference electrodes



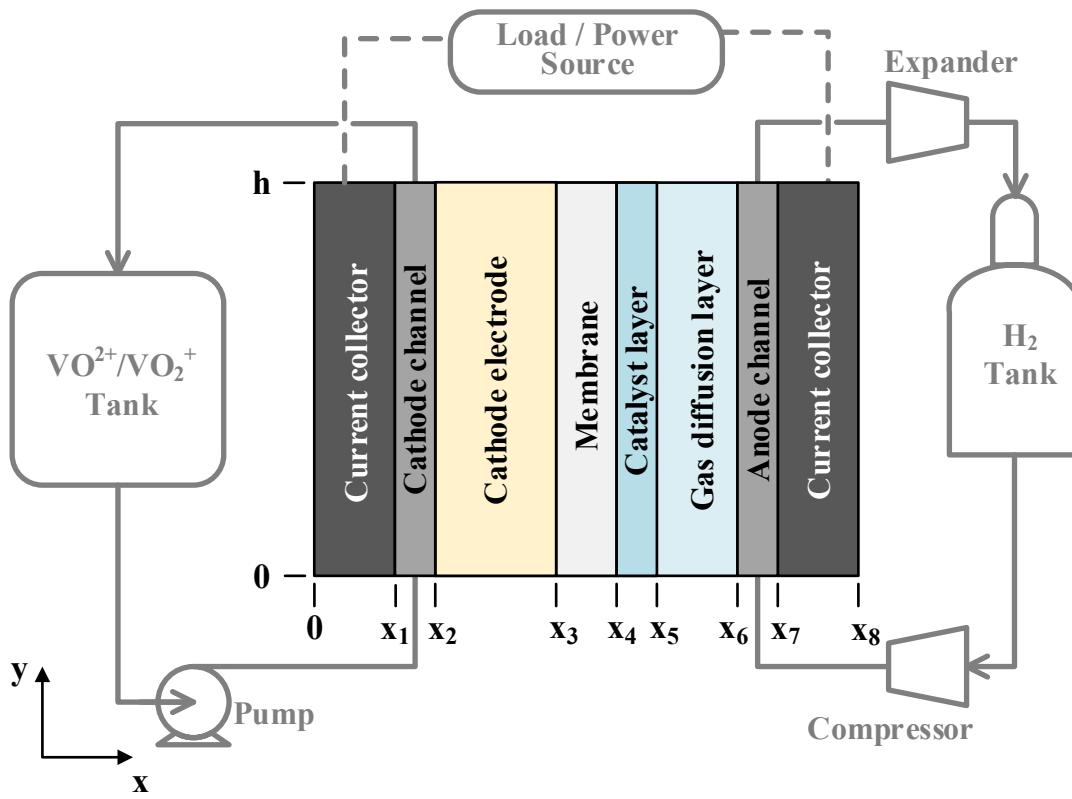
Cell 2: 50% SOC, $Q_V=77 \text{ mL min}^{-1}$, $Q_{H_2}=100 \text{ mL min}^{-1}$



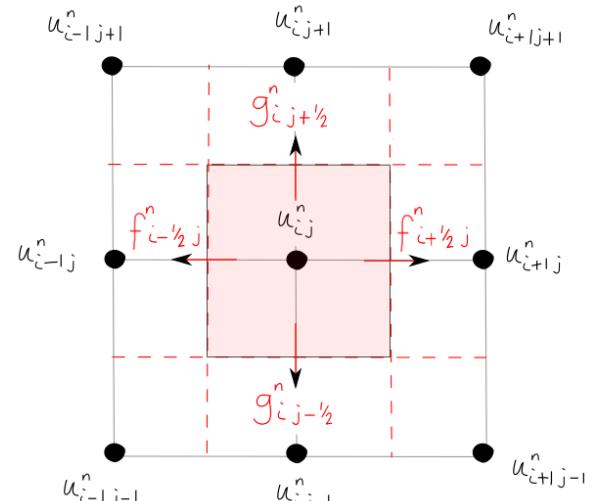
Cell 2: 100% SOC, $Q_V=77 \text{ mL min}^{-1}$, $Q_{H_2}=100 \text{ mL min}^{-1}$



2D continuum model

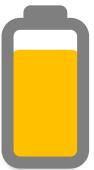


- Finite volume method

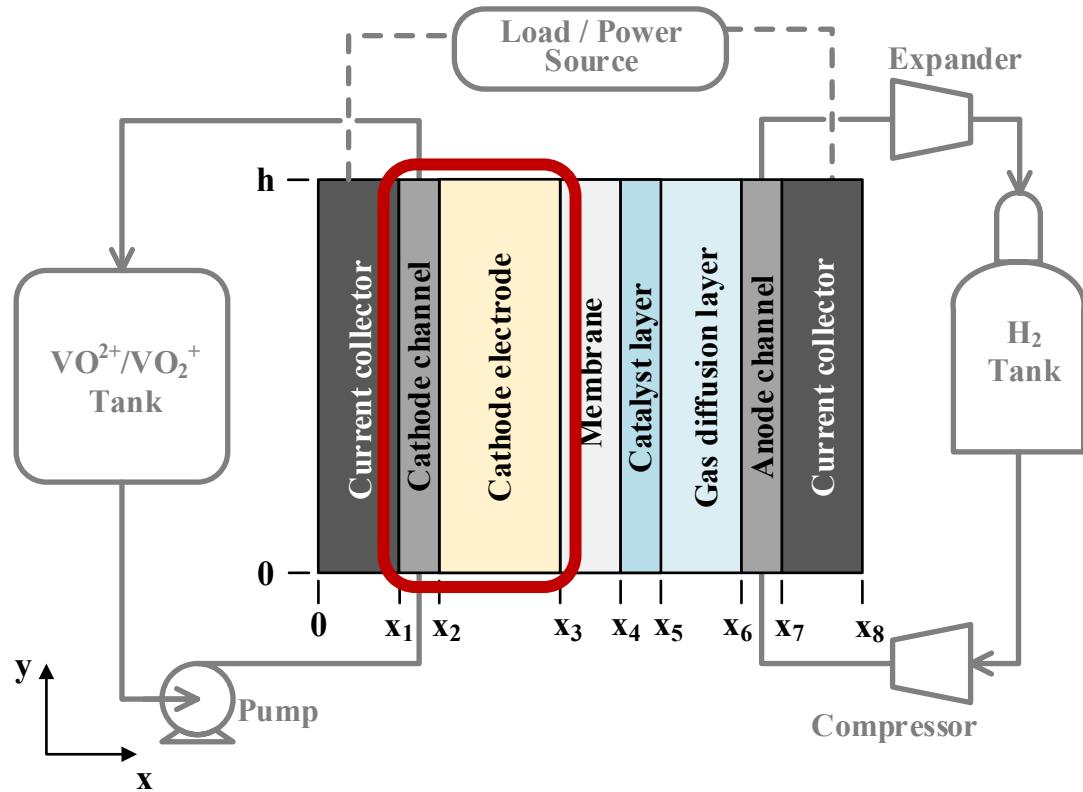


$$\frac{\partial u}{\partial t} + \nabla \cdot F = q$$

$$\frac{\partial}{\partial t} \frac{1}{h^2} \int_{I_{ij}} u dx dy + \frac{1}{h^2} \oint_{I_{ij}} (F \cdot n) dS = \frac{1}{h^2} \int_{I_{ij}} u dx dy$$

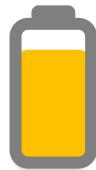


2D continuum model



Model implementation

- Visual Studio C++
- Semi-implicit FVM
- CGM optimization



Model summary

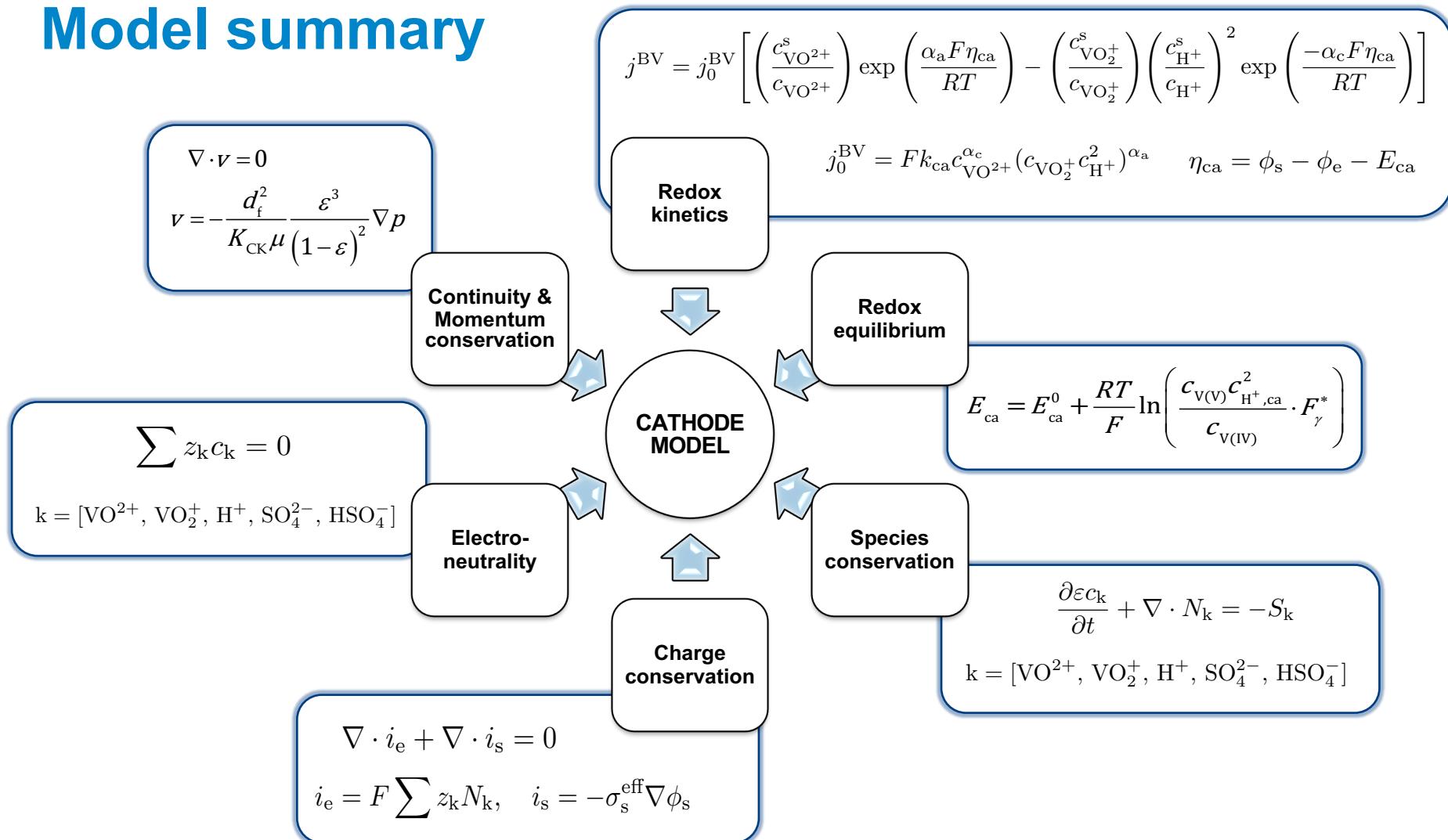
$$V = -\frac{d_f^2}{K_{CK}\mu} \frac{\varepsilon^3}{(1-\varepsilon)^2} \nabla p$$

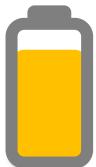
$$\sum z_k c_k = 0$$

$$k = [\text{VO}^{2+}, \text{VO}_2^+, \text{H}^+, \text{SO}_4^{2-}, \text{HSO}_4^-]$$

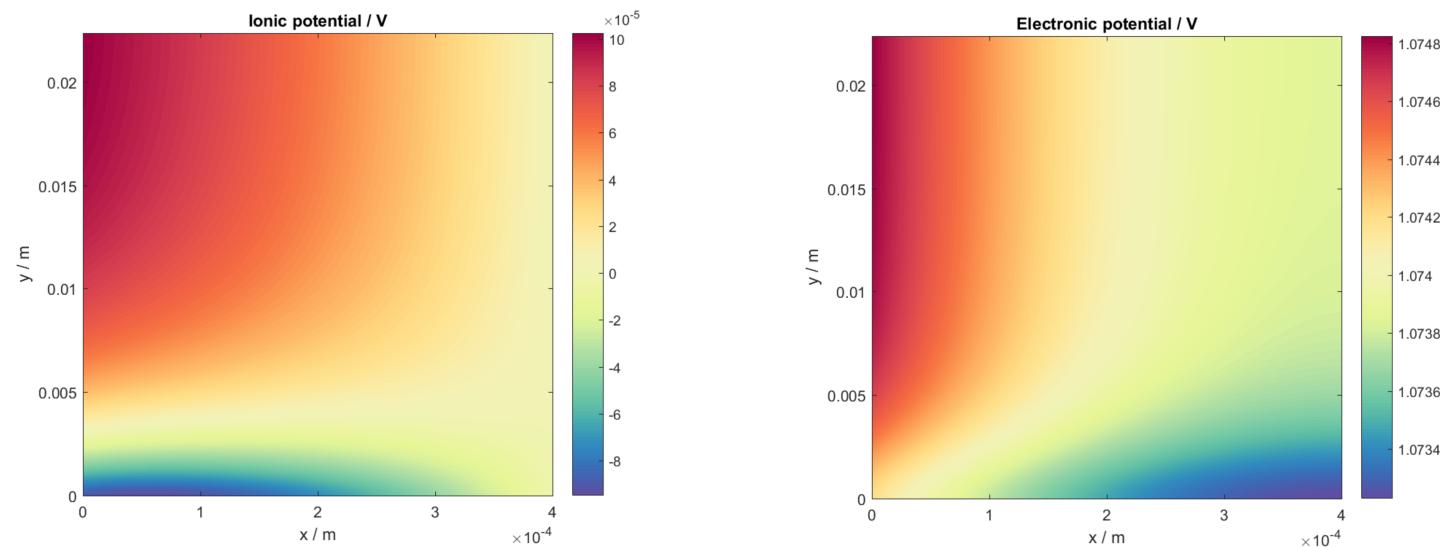
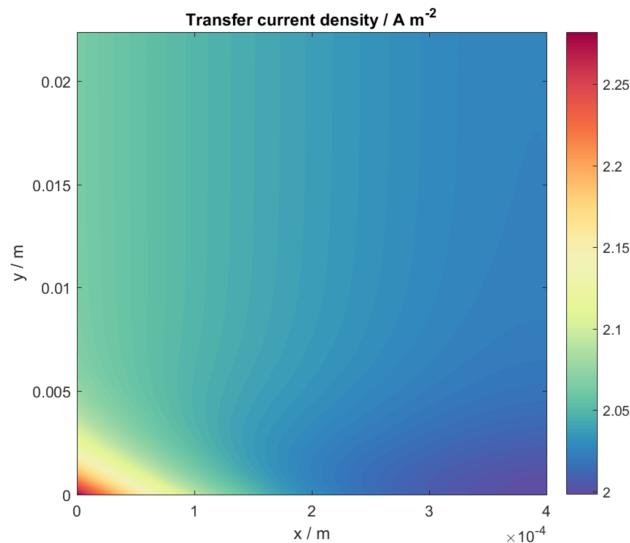
$$\nabla \cdot i_e + \nabla \cdot i_s = 0$$

$$i_e = F \sum z_k N_k, \quad i_s = -\sigma_s^{\text{eff}} \nabla \phi_s$$



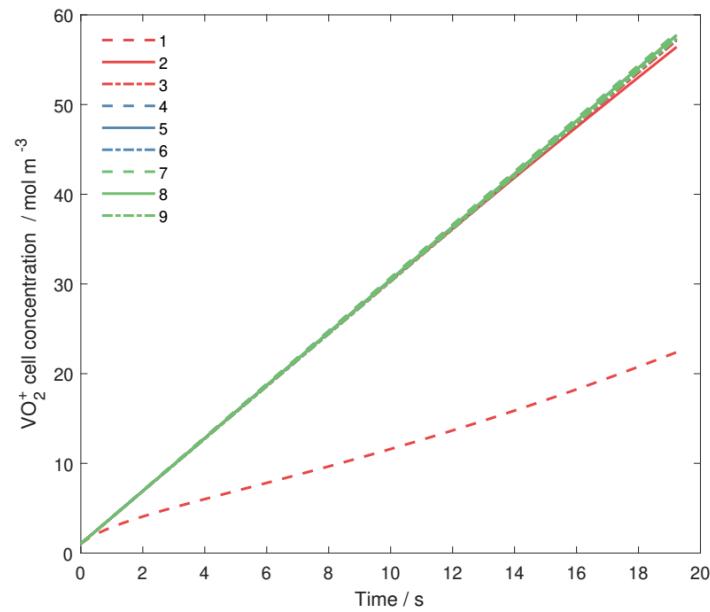
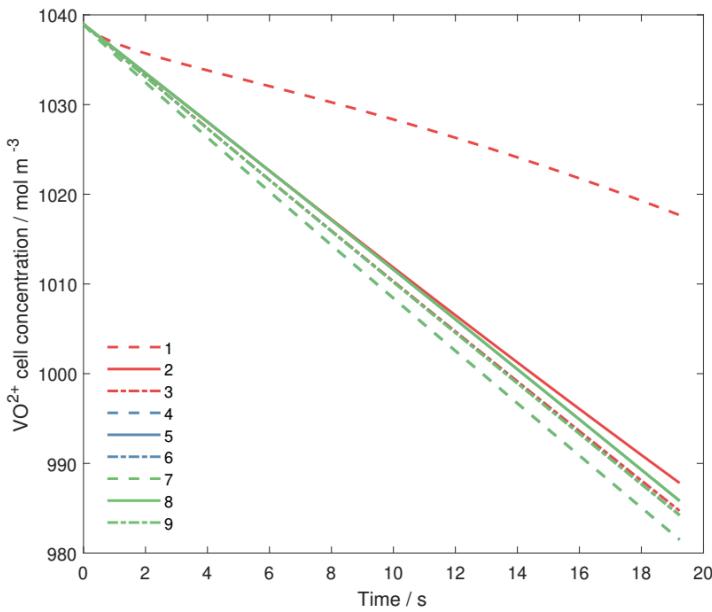
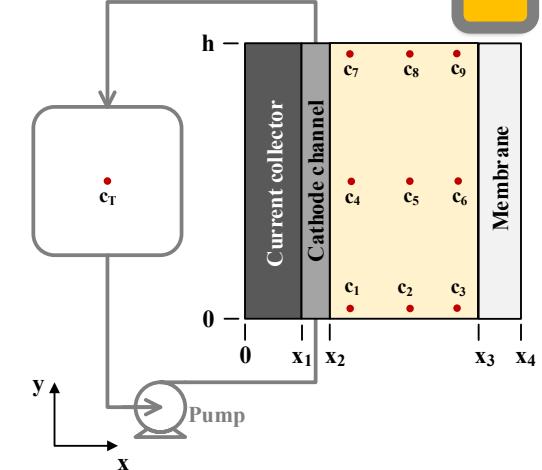
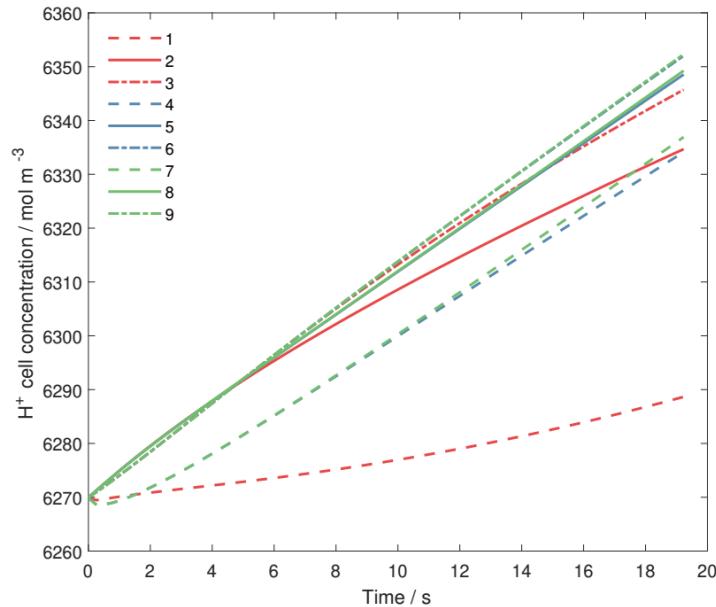


Preliminary results



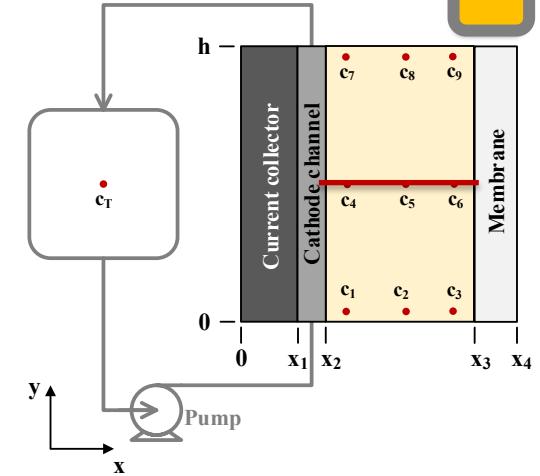
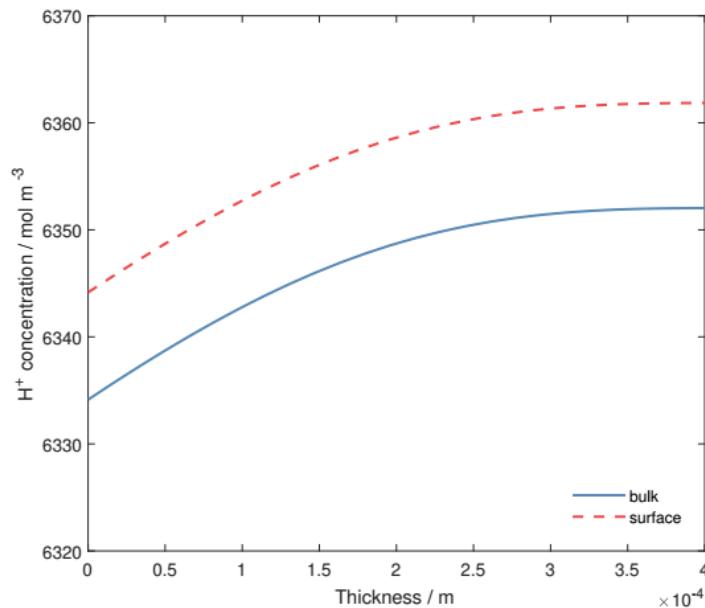
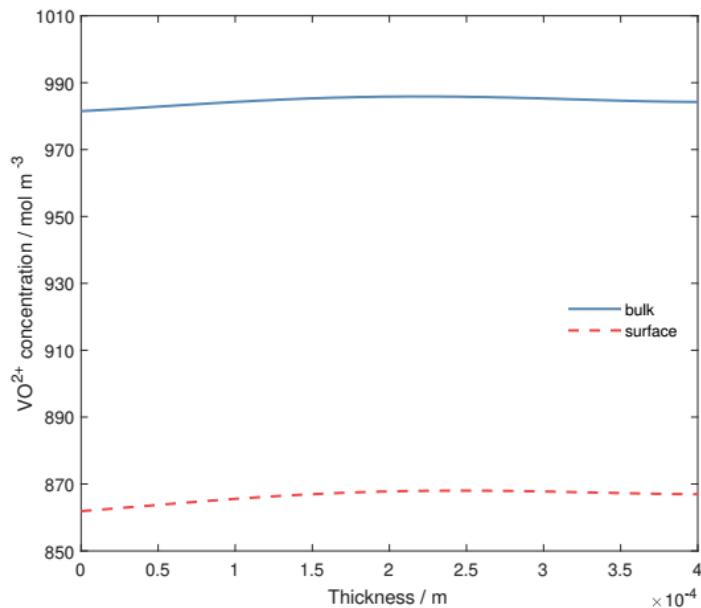
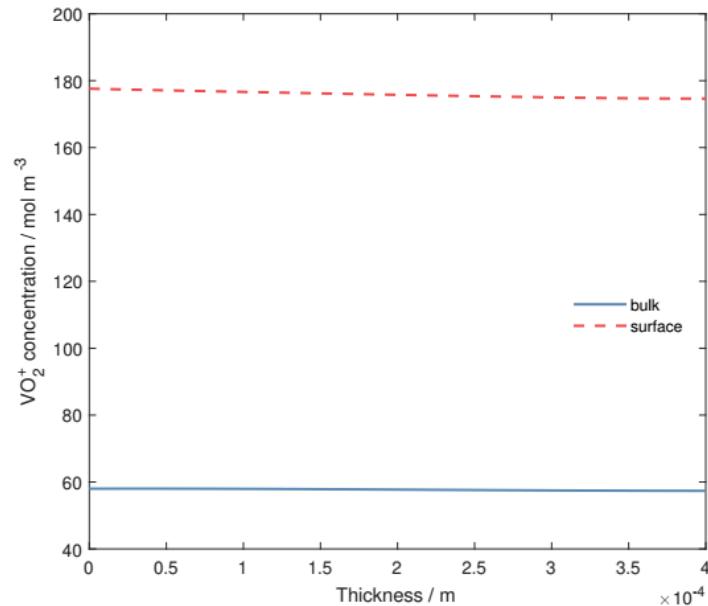


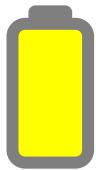
Species concentration





Species concentration



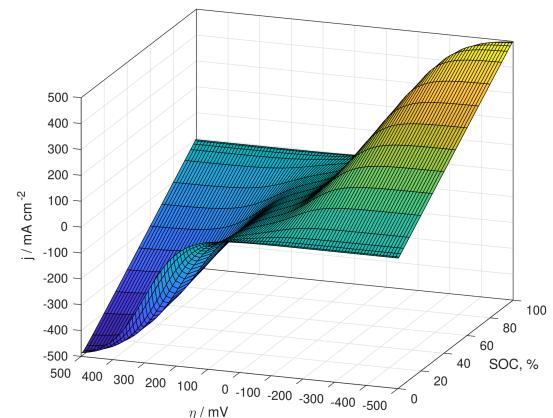


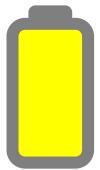
Conclusions

- A unit cell model for a VRFB was validated against literature data.
- A complete Nernst equation based on thermodynamic principles was proposed and fit to the OCP data.
- A complete Butler-Volmer kinetic equation was proposed for the cathode, considering the effect of protons concentration.

Thermodynamic derivation of CNE

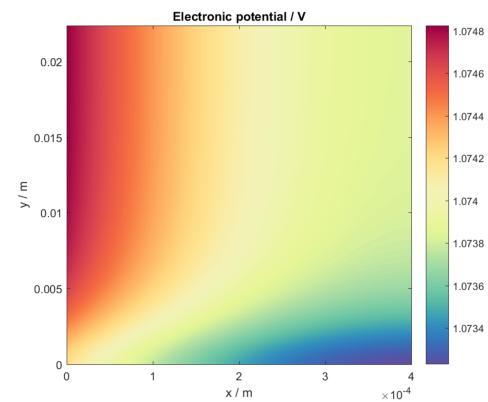
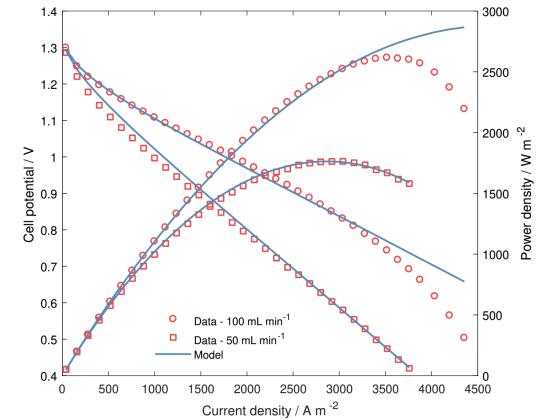
$$E_{OCP} = E_{cell}^0 + \frac{RT}{F} \ln \left(\frac{c_{VO_2^{+}}^{ca} (c_{H^{+}}^{ca})^2 (p_{H_2}^g)^{0.5}}{c_{VO^{2+}}^{ca} c_{H^{+}}^{an}} \times \frac{c_{H^{+}}^{an}}{c_{H^{+}}^{ca}} \times F \gamma \right)$$

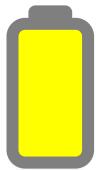




Conclusions

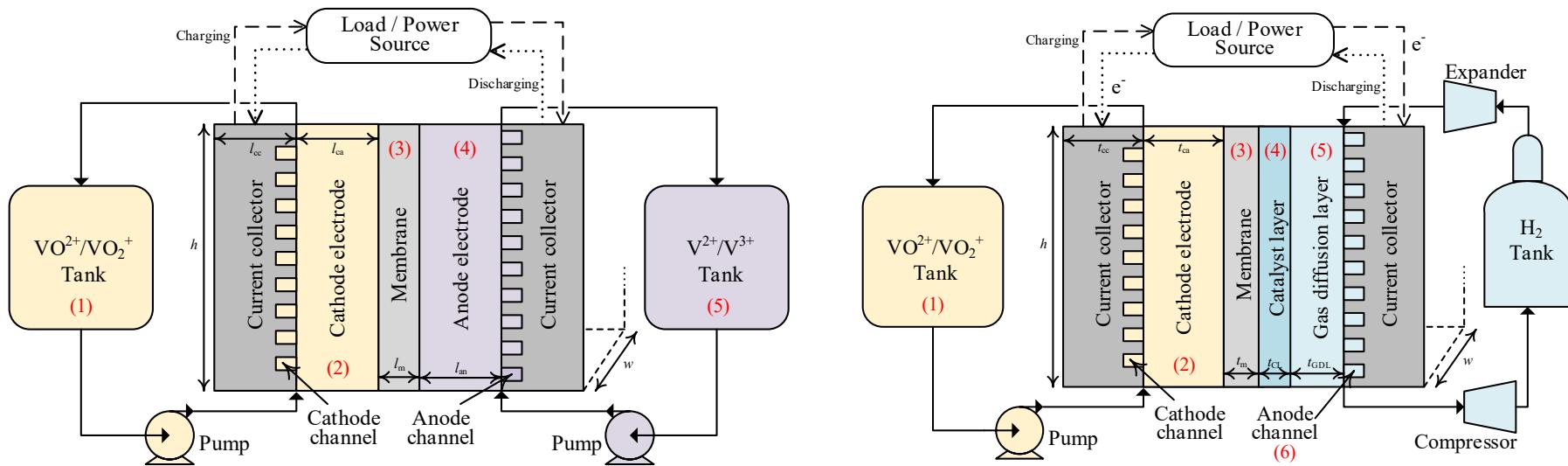
- A unit cell model for a RHVFC was introduced and calibrated against experimental data from 3 different devices.
- Well fitted polarization curves for the range of current density validated.
- An initial 2D model of the cathode was introduced.

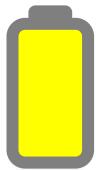




Next steps – unit cell models

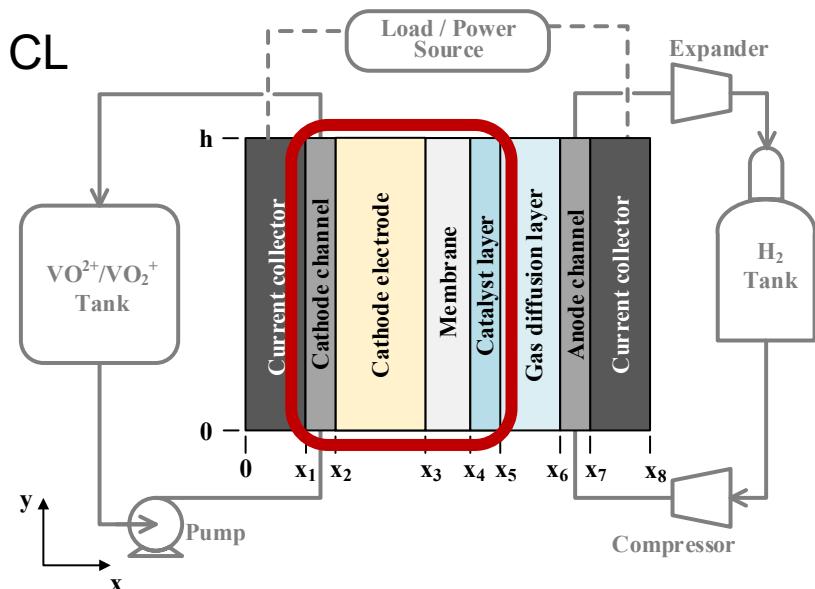
- To better validate (anode + membrane) potential from reference electrodes
- Performance comparison of VRFB and RHVFC
- Parameter sensitivity studies





Next steps – 2D continuum model

- Distributed model for the Membrane and CL
- Cross-over of ionic species
- Dominant transport phenomena
- Overpotential contributions



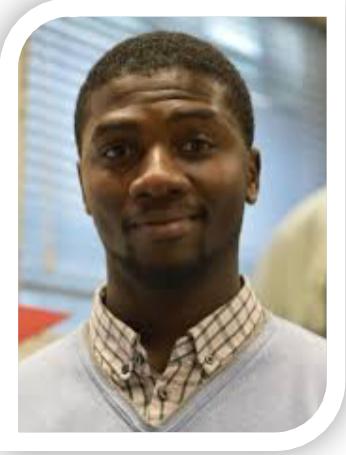
Acknowledgements



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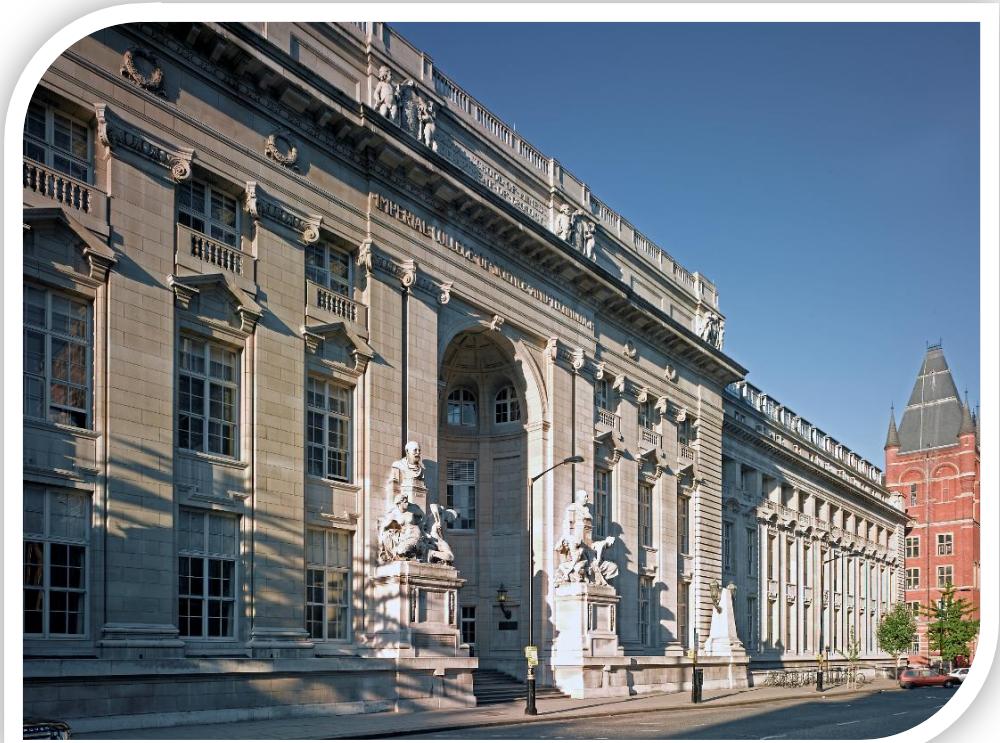
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Prof. Nigel Brandon

**Electrochemical Science and
Engineering Group**

Engineering and Physical Sciences
Research Council



Thank you!

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